## MAT 171 Sample Final Exam

General Instructions: Answer each question in the book provided. Partial credit will be given, so show all of your work and label each of your graphs with at least 3 coordinates. Calculators are NOT permitted.

Scoring. Problems 1-12 are worth 4 credits each. Problems 13 and 14 are worth 5 credits each. Problems 15 and 16 are worth 6 credits each.

1. Let $f(x)=x+5$ and let $g(x)=x^{2}+5 x$. Specify the domain of $f(x) / g(x)$.
2. Simplify: $\frac{\frac{4}{x-6}-\frac{4}{x+6}}{\frac{8}{x^{2}-36}}$
3. Draw the graph of $|x-2|+4$.
4. Write an equation of the line perpendicular to the line $y=3 x-7$ at $(5,8)$.
5. Draw the graph of $y=3 x^{2}+6 x-24$ and label its minimum.
6. Draw the graph of $\sqrt{x+4}$.
7. Write an equation of the line given the graph in Figure A on the back of this page.
8. Write an equation of the parabola given its graph in Figure B on the back of this page.
9. Let $g(x)=\frac{x-6}{3 x+1}$. Write the inverse of $g$ and specify its domain.
10. Simplify by using polynomial long division $\frac{x^{3}+4 x^{2}-2 x+8}{x-2}$.
11. Solve for $x: \quad 4 e^{3 x+7}=128$
12. Let $f(x)=3 x^{2}+7$. Compute and simplify the difference quotient given by $\frac{f(x+h)-f(x)}{h}$.
13. Draw the graph of $f(x)=\frac{x-3}{x^{2}-49}$. Indicate asymptotes.
14. Draw the graph of $F(x)= \begin{cases}10-5 x, & \text { for } x<1 \\ 5 x-10, & \text { for } x \geq 1\end{cases}$
15. Use $f(x)=\log _{5}(2 x-1)$ to address the following problems.
(a) Find the domain of $f$.
(b) Compute $f(1)$.
(c) Find the number $a$ so that $f(a)=2$.
16. If 40 people contribute to a performance space, then each pays $\$ 100$. For every $\$ 1$ less that people pay, 4 additional people contribute. USE AN EQUATION to determine the maximum amount of money that can be raised.

## Figures On Back



Figure A


Figure B

