NATIONAL RECOGNITION REPORT
Initial Preparation of Mathematics Teachers at the Secondary Level (2012 Standards)

National recognition of this program is dependent on the review of the program by representatives of the National Council of Teachers of Mathematics (NCTM).

COVER PAGE

Name of Institution
Lehman College - CUNY School of Education, NY

Date of Review

MM  DD  YYYY
02  01  2021

This report is in response to a(n):
○ Initial Review
○ Revised Report
○ Response to Conditions Report

Program Covered by this Review
Mathematics Education (G)

Grade Level
7-12

(1) e.g. Early Childhood; Elementary K-6

Program Type
First teaching license

Award or Degree Level
○ Baccalaureate
○ Post Baccalaureate
○ Master's

PART A - RECOGNITION DECISION

SPA decision on national recognition of the program(s):
○ Nationally recognized
○ Nationally recognized with conditions
○ Further development required OR Nationally recognized with probation OR Not nationally recognized [See Part G]

Test Results (from information supplied in Assessment #1, if applicable)
The program meets or exceeds SPA benchmarked licensure test data requirement, if applicable:
○ Yes
○ No
○ Not applicable
○ Not able to determine

Comments, if necessary, concerning Test Results:
Under CAEP, there is no stated policy and no CAEP standard stating an 80% pass rate requirement on licensure tests. Additional information can be found at http://www.caepnet.org/accreditation/caep-accreditation/spa-program-review-process/data-requirements-for-spa-review.

Summary of Strengths:
The field experiences and student teaching provide candidates opportunities to engage with students from diverse backgrounds including ethnic and cultural differences, socioeconomically disadvantaged students, students who are English language learners, and students with exceptionalities.

PART B - STATUS OF MEETING SPA STANDARDS

Standard 1: Content Knowledge

Effective teachers of secondary mathematics demonstrate and apply knowledge of major mathematics concepts, algorithms, procedures, connections, and applications within and among mathematical content domains.

Preservice teacher candidates:
1a) Demonstrate and apply knowledge of major mathematics concepts, algorithms, procedures, applications in varied contexts, and connections within and among mathematical domains (Number, Algebra, Geometry, Trigonometry, Statistics, Probability, Calculus, and Discrete Mathematics) as outlined in the NCTM Mathematics Content for Secondary.

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Standard 1 Comments:
State-required licensure test(s) aligned to NCTM CAEP Mathematics Content for Secondary and at least one additional assessment collectively demonstrating at least an 80% alignment to each domain of the NCTM CAEP Mathematics Content for Secondary providing evidence that Element 1a* is met at the acceptable or target level are required in order to satisfy the preponderance of evidence for Standard 1.

*: Indicates essential (required) element

Section III of the program report indicates Assessments 1 and 2 address this standard.

*Element 1a: MET

Assessment 1 (NY CST 04/004) continues to provide evidence for the mathematical domain competencies specified in the NCTM CAEP Mathematics Content for Secondary alignment on the NCTM website (www.nctm.org/caep) and noted in the Feedback section below. Because the completers were allowed to take the older "safety net" version or the revised version during this round of data, reviewers have accepted the assessment as evidence for indicators officially aligned by the NCTM to either exam.

Assessment 2 (Course Grades) provides evidence for the mathematical domain competencies noted in the Feedback section below.

Feedback on the NCTM CAEP Mathematics Content for Secondary alignment:
A.1 Number and Quantity Competencies SATISFIED (At least 80% competency alignment)
Competencies A.1.1, A.1.2, A.1.3, and A.1.4 were met in the 8/1/2020 Recognition Report by Assessment 1. Assessment 1 (NY CST 04/004) continues to provide evidence for A.1.1, A.1.2, A.1.3, and A.1.4.
Assessment 2 (Course Grades) provides evidence for A.1.1 (MAT 615, 637, 604), A.1.2 (MAT 615 637, 605), A.1.3 (MAT 175, 176), A.1.4 (MAT 601), and A.1.5 (MAT 661).

A.2 Algebra Competencies SATISFIED (At least 80% competency alignment)
Competencies A.2.1, A.2.2, A.2.3, A.2.4, and A.2.6 were met in the 8/1/2020 Recognition Report by Assessment 1. Assessment 1 (NY CST 04/004) continues to provide evidence for A.2.1, A.2.2, A.2.3, A.2.4, and A.2.6.
Assessment 2 (Course Grades) provides evidence for A.2.1 (MAT 175, 176, 637, 604, 655), A.2.2 (MAT 175, 176, 637, 655, 601), A.2.3 (MAT 175, 176, 647, 601, 604, 655), A.2.4 (MAT 175, 176, 637 601), A.2.5 (MAT 601, 615), A.2.6 (MAT 615) and A.2.7 (MAT 661).

A.3 Geometry and Trigonometry Competencies SATISFIED (At least 80% competency alignment)
Assessment 2 (Course Grades) provides evidence for A.3.1 (MAT 601, 655), A.3.2 (MAT 601, 615, 655), A.3.3 (MAT 601, 615, 655), A.3.4 (MAT 601, 176), A.3.5 (MAT 601, 175, 176), A.3.6 (MAT 601, 655), A.3.7 (MAT 601), A.3.8 (MAT 601, 655), A.3.9 (MAT 601, 655) and A.3.10 (MAT 661).

A.4 Statistics and Probability Competencies SATISFIED (At least 80% competency alignment)
Competencies A.4.3, A.4.4, and A.4.5 were met in the 8/1/2020 Recognition Report by Assessment 1. Assessment 1 (NY CST 04/004) continues to provide evidence for A.4.3, A.4.4, and A.4.5.
Assessment 2 (Course Grades) provides evidence for A.4.1 (MAT 637, 655), A.4.4 (MAT 637, 655), A.4.5 (MAT 601, 655) and A.4.6 (MAT 661). There is partial evidence for A.4.2 (MAT 637 does not address creation of surveys, sampling methods, or statistical design). There is insufficient evidence for A.4.3 (MAT 637 does not clearly address the competency).

A.5 Calculus Competencies SATISFIED (At least 80% competency alignment)
Competencies A.5.1, A.5.3 and A.5.4 were met in the 8/1/2020 Recognition Report by Assessment 2. Assessment 1 (NY CST 04/004) continues to provide evidence for A.5.1, A.5.3, and A.5.5.
Assessment 2 (Course Grades) provides evidence for A.5.1 (MAT 175, 176, 655), A.5.2 (MAT 601), A.5.3 (MAT 175, 604, 655), A.5.4 (MAT 601), A.5.5 (MAT 175, 176), and A.5.6 (MAT 661).
A.6 Discrete Mathematics Competencies SATISFIED (At least 80% competency alignment)
Competencies A.6.2, A.6.3, and A.6.4 were met in the 8/1/2020 Recognition Report by Assessment 1.
Assessment 1 (NY CST 04/004) continues to provide evidence for A.6.2, A.6.3, and A.6.4.
Assessment 2 (Course Grades) provides evidence for A.6.2. (MAT 637), A.6.3 (MAT 637, 601), A.6.4 (MAT 637), and A.6.5 (MAT 661, 637). MAT 637 gives partial evidence for A.6.1 (does not address graphs, trees, and networks).

Standard 2: Mathematical Practices

Effective teachers of secondary mathematics solve problems, represent mathematical ideas, reason, prove, use mathematical models, attend to precision, identify elements of structure, generalize, engage in mathematical communication, and make connections as essential mathematical practices. They understand that these practices intersect with mathematical content and that understanding relies on the ability to demonstrate these practices within and among mathematical domains and in their teaching.

Preservice teacher candidates:
2a) Use problem solving to develop conceptual understanding, make sense of a wide variety of problems and persevere in solving them, apply and adapt a variety of strategies in solving problems confronted within the field of mathematics and other contexts, and formulate and test conjectures in order to frame generalizations.
2b) Reason abstractly, reflectively, and quantitatively with attention to units, constructing viable arguments and proofs, and critiquing the reasoning of others; represent and model generalizations using mathematics; recognize structure and express regularity in patterns of mathematical reasoning; use multiple representations to model and describe mathematics; and utilize appropriate mathematical vocabulary and symbols to communicate mathematical ideas to others.
2c) Formulate, represent, analyze, and interpret mathematical models derived from real-world contexts or mathematical problems.
2d) Organize mathematical thinking and use the language of mathematics to express ideas precisely, both orally and in writing to multiple audiences.
2e) Demonstrate the interconnectedness of mathematical ideas and how they build on one another and recognize and apply mathematical connections among mathematical ideas and across various content areas and real-world contexts.
2f) Model how the development of mathematical understanding within and among mathematical domains intersects with the mathematical practices of problem solving, reasoning, communicating, connecting, and representing.

Met Met with Conditions Not Met

Standard 2 Comments:
In order to satisfy the preponderance of evidence for Standard 2, Elements 2a*, 2b*, and at least 2 additional elements must be met at the acceptable or target level; at least two assessments must provide collective evidence for the overall Standard.
*: Indicates essential (required) elements

Section III of the program report indicates Assessments 2, 3, 6, and 7 address this standard.

*Element 2a: MET
Element 2a was met in the 8/1/2020 Recognition Report by Assessment 6.
Assessment 2 (Course Grades) provides evidence for Element 2a.

*Element 2b: MET
Element 2b was met in the 8/1/2020 Recognition Report by Assessment 6.
Assessment 2 (Course Grades) provides evidence for Element 2b.

Element 2c: MET
Element 2c was met in the 8/1/2020 Recognition Report by Assessment 6.
Assessment 2 (Course Grades) provides evidence for Element 2c.

Element 2d: MET
Element 2d was met in the 8/1/2020 Recognition Report by Assessment 6.
Assessment 2 (Course Grades) provides evidence for Element 2d.

Element 2e: MET
Element 2e was met in the 8/1/2020 Recognition Report by Assessment 6.
Assessment 2 (Course Grades) provides evidence for Element 2e.

Element 2f: MET
Element 2f was met in the 8/1/2020 Recognition Report by Assessment 6.
Assessment 2 (Course Grades) provides evidence for Element 2f.

Standard 3: Content Pedagogy

Effective teachers of secondary mathematics apply knowledge of curriculum standards for mathematics and their relationship to student learning within and across mathematical domains. They incorporate research-based mathematical experiences and include multiple instructional strategies and mathematics-specific technological tools in their teaching to develop all students’ mathematical understanding and proficiency. They provide students with opportunities to do mathematics – talking about it and connecting it to both theoretical and real-world contexts. They plan, select, implement, interpret, and use formative and summative assessments for monitoring student learning, measuring student mathematical understanding, and informing practice.

Preservice teacher candidates:
3a) Apply knowledge of curriculum standards for secondary mathematics and their relationship to student learning within and across mathematical domains.
3b) Analyze and consider research in planning for and leading students in rich mathematical learning experiences.
3c) Plan lessons and units that incorporate a variety of strategies, differentiated instruction for diverse populations, and mathematics-specific and instructional technologies in building all students’ conceptual understanding and procedural proficiency.
3d) Provide students with opportunities to communicate about mathematics and make connections among mathematics, other content areas, everyday life, and the workplace.
3e) Implement techniques related to student engagement and communication including selecting high quality tasks, guiding mathematical discussions, identifying key mathematical ideas, identifying and addressing student misconceptions, and employing a range of questioning strategies
3f) Plan, select, implement, interpret, and use formative and summative assessments to inform instruction by reflecting on mathematical proficiencies essential for all students.
3g) Monitor students’ progress, make instructional decisions, and measure students’ mathematical understanding and ability using formative and summative assessments.

Met Met with Conditions Not Met

Standard 3 Comments:
In order to satisfy the preponderance of evidence for Standard 3, Elements 3a*, 3c*, 3f* and at least 1 additional element must be met at the acceptable or target level; at least two assessments must provide collective evidence for the overall Standard.
*: Indicates essential (required) elements

Section III of the program report indicates Assessments 3, 4, 5, 6, and 7 address this standard.

*Element 3a: MET
Element 3a was met in the 8/1/2020 Recognition Report by Assessment 6.

Element 3b: MET
Element 3b was met in the 8/1/2020 Recognition Report by Assessments 3, 5, and 6.

*Element 3c: MET
Element 3c was met in the 8/1/2020 Recognition Report by Assessment 5.

Element 3d: MET
Element 3d was met in the 8/1/2020 Recognition Report by Assessment 6.

Element 3e: MET
Element 3e was met in the 8/1/2020 Recognition Report by Assessment 6.

*Element 3f: MET
Element 3f was met in the 8/1/2020 Recognition Report by Assessments 3, 5 and 6.

Element 3g: MET
Element 3g was met in the 8/1/2020 Recognition Report by Assessments 5 and 6.

**Standard 4: Mathematical Learning Environment**

Effective teachers of secondary mathematics exhibit knowledge of adolescent learning, development, and behavior. They use this knowledge to plan and create sequential learning opportunities grounded in mathematics education research where students are actively engaged in the mathematics they are learning and building from prior knowledge and skills. They demonstrate a positive disposition toward mathematical practices and learning, include culturally relevant perspectives in teaching, and demonstrate equitable and ethical treatment of and high expectations for all students. They use instructional tools such as manipulatives, digital tools, and virtual resources to enhance learning while recognizing the possible limitations of such tools.

Preservice teacher candidates:
4a) Exhibit knowledge of adolescent learning, development, and behavior and demonstrate a positive disposition toward mathematical processes and learning.
4b) Plan and create developmentally appropriate, sequential, and challenging learning opportunities grounded in mathematics education research in which students are actively engaged in building new knowledge from prior knowledge and experiences.
4c) Incorporate knowledge of individual differences and the cultural and language diversity that exists within classrooms and include culturally relevant perspectives as a means to motivate and engage students.
4d) Demonstrate equitable and ethical treatment of and high expectations for all students.
4e) Apply mathematical content and pedagogical knowledge to select and use instructional tools such as manipulatives and physical models, drawings, virtual environments, spreadsheets, presentation tools, and mathematics-specific technologies (e.g., graphing tools, interactive geometry software, computer algebra systems, and statistical packages); and make sound decisions about when such tools enhance teaching and learning, recognizing both the insights to be gained and possible limitations of such tools.

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**Standard 4 Comments:**
In order to satisfy the preponderance of evidence for Standard 4, Elements 4b*, 4d*, and 4e* must be met at the acceptable or target level; at least two assessments must provide collective evidence for the overall Standard.
*: Indicates essential (required) elements

Section III of the program report indicates Assessments 3, 4, 5, 7, and 8 address this standard.

Element 4a: NOT MET
Assessment 4 (STEF) provides partial evidence for Element 4a (does not address positive disposition).

*Element 4b: MET
Assessment 4 (STEF) provides evidence for Element 4b.

Element 4c: MET
Element 4c was met in the 8/1/2020 Recognition Report by Assessments 4 and 5. Assessment 4 (STEF) continues to provide evidence for Element 4c.

*Element 4d: MET
Element 4d was met in the 8/1/2020 Recognition Report by Assessment 4. Assessment 4 (STEF) continues to provide evidence for Element 4d. Assessment 5 (Impact on Student Learning) provides evidence for Element 4d.

*Element 4e: MET
Assessment 4 (STEF) provides evidence for Element 4e.

**Standard 5: Impact on Student Learning**

**Effective teachers of secondary mathematics provide evidence demonstrating that as a result of their instruction, secondary students’ conceptual understanding, procedural fluency, strategic competence, adaptive reasoning, and application of major mathematics concepts in varied contexts have increased. These teachers support the continual development of a productive disposition toward mathematics. They show that new student mathematical knowledge has been created as a consequence of their ability to engage students in mathematical experiences that are developmentally appropriate, require active engagement, and include mathematics-specific technology in building new knowledge.**

Preservice teacher candidates:
5a) Verify that secondary students demonstrate conceptual understanding; procedural fluency; the ability to formulate, represent, and solve problems; logical reasoning and continuous reflection on that reasoning; productive disposition toward mathematics; and the application of mathematics in a variety of contexts within major mathematical domains.
5b) Engage students in developmentally appropriate mathematical activities and investigations that require active engagement and include mathematics-specific technology in building new knowledge.
5c) Collect, organize, analyze, and reflect on diagnostic, formative, and summative assessment evidence and determine the extent to which students’ mathematical proficiencies have increased as a result of their instruction.

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*Standard 5 Comments:*

In order to satisfy the preponderance of evidence for Standard 5, Element 5c* and at least 1 additional element must be met at the acceptable or target level; at least two assessments must provide collective evidence for the overall Standard.

*: Indicates essential (required) elements

Section III of the program report indicates Assessments 3, 4, 5, and 7 address this standard.

Element 5a: MET
Element 5a was met in the 8/1/2020 Recognition Report by Assessment 5. Assessment 5 (Impact on Student Learning) continues to provide evidence for Element 5a.

Element 5b: MET
Element 5b was met in the 8/1/2020 Recognition Report by Assessments 4 and 5. Assessment 5 (Impact on Student Learning) continues to provide evidence for Element 5b.

*Element 5c: MET
Element 5c was met in the 8/1/2020 Recognition Report by Assessment 5. Assessment 5 (Impact on Student Learning) continues to provide evidence for Element 5c.

**Standard 6: Professional Knowledge and Skills**
Effective teachers of secondary mathematics are lifelong learners and recognize that learning is often collaborative. They participate in professional development experiences specific to mathematics and mathematics education, draw upon mathematics education research to inform practice, continuously reflect on their practice, and utilize resources from professional mathematics organizations.

Preservice teacher candidates:
6a) Take an active role in their professional growth by participating in professional development experiences that directly relate to the learning and teaching of mathematics.
6b) Engage in continuous and collaborative learning that draws upon research in mathematics education to inform practice; enhance learning opportunities for all students' mathematical knowledge development; involve colleagues, other school professionals, families, and various stakeholders; and advance their development as a reflective practitioner.
6c) Utilize resources from professional mathematics education organizations such as print, digital, and virtual resources/collections.

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**Standard 6 Comments:**

In order to satisfy the preponderance of evidence for Standard 6, Element 6b* and at least 1 additional element must be met at the acceptable or target level; at least two assessments must provide collective evidence for the overall Standard.

*: Indicates essential (required) elements

Section III of the program report indicates Assessments 4, 5, and 8 address this standard.

Element 6a: MET
Assessment 4 (STEF) provides evidence for Element 6a.

*Element 6b: MET
Assessment 4 (STEF) provides partial evidence for Element 6b. Only distinguished and proficient levels address use of research to inform practice; does not address enhancing all students' knowledge of mathematics or involving stakeholders. For this element, Assessment 4 employs a generic rubric that does not address specific NCTM elements or sub-elements.

Assessment 5 (Impact on Student Learning) new elements provide evidence for Element 6b.

Element 6c: MET
Assessment 4 (STEF) provides evidence for Element 6c.
Assessment 8 (Portfolio) provides evidence for Element 5c.

**Standard 7: Secondary Mathematics Field Experiences and Clinical Practice**

Effective teachers of secondary mathematics engage in a planned sequence of field experiences and clinical practice under the supervision of experienced and highly qualified mathematics teachers. They develop a broad experiential base of knowledge, skills, effective approaches to mathematics teaching and learning, and professional behaviors across both middle and high school settings that involve a diverse range and varied groupings of students. Candidates experience a full-time student teaching/internship in secondary mathematics directed by university or college faculty with secondary mathematics teaching experience or equivalent knowledge base.

Preservice teacher candidates:
7a) Engage in a sequence of planned field experiences and clinical practice prior to a full-time student teaching/internship experience that include observing and participating in both middle and high school mathematics classrooms and working with a diverse range of students individually, in small groups, and in large class settings under the supervision of experienced and highly qualified mathematics teachers in varied settings that reflect cultural, ethnic, linguistic, gender, and learning differences.
7b) Experience full-time student teaching/internship in secondary mathematics that is supervised by a highly qualified mathematics teacher and a university or college supervisor with secondary mathematics teaching experience or equivalent knowledge base.
7c) Develop knowledge, skills, and professional behaviors across both middle and high school settings; examine the nature of
mathematics, how mathematics should be taught, and how students learn mathematics; and observe and analyze a range of approaches to mathematics teaching and learning, focusing on tasks, discourse, environment, and assessment.

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| Information included in Section I - Context #2 of the program report for Element 7a* and in Section I - Context #2 and #6 for Element 7b* and at least one assessment for Element 7c* providing evidence that Elements 7a*, 7b*, and 7c* are met at the acceptable or target level are required in order to satisfy the preponderance of evidence for Standard 7.

*: Indicates essential (required) elements

*Element 7a: MET
Candidates participate in early field experiences in middle and high school settings, supervised by experienced and highly qualified mathematics teachers, in a variety of settings and with as diverse range of students.

*Element 7b: MET
Candidates experience full-time student teaching in secondary mathematics, supervised by experienced and highly qualified mathematics teachers by a college supervisor with secondary teaching experience.

Section III of the program report indicates Assessments 4, 5, and 8 address Element 7c*.

*Element 7c: MET
Assessment 4 (STEF) provides evidence for Element 7c.
Assessment 8 (Portfolio) provides evidence for Element 7c.

PART C - EVALUATION OF PROGRAM REPORT EVIDENCE

C.1. Candidates’ knowledge of content
Assessment 1 (NY CST 04/004) and revised course descriptions in Assessment 2 (Course Grades) provide sufficient evidence of candidates’ content knowledge. Assessments 3 (Curriculum Unit), 6 (Problem Solving Episode), and 7 (ESC 740 Exams) collectively provide evidence for the candidate mathematical practices (Standard 2).

C.2. Candidates’ ability to understand and apply pedagogical and professional content knowledge, skills, and dispositions
Assessment 3 (Plan for Instruction), 4 (STEF), 6 (Problem Solving Episode), and new Assessment 8 (Portfolio) address candidates’ ability to understand and apply pedagogical and professional content knowledge, and skills and dispositions. Additional rubric elements for Assessment 4 provide evidence for previously unmet elements. Assessments 3 and 6 were not resubmitted.

C.3. Candidate effects on P-12 student learning
Assessments 3 (Plan for Instruction), 4 (Student Teacher Observation Evaluation), and 5 (Impact on Student Learning) continue to provide sufficient evidence of candidate effects on P-12 student learning.
**PART D - EVALUATION OF THE USE OF ASSESSMENT RESULTS**

Evidence that assessment results are evaluated and applied to the improvement of candidate performance and strengthening of the program (as discussed in Section V of the program report)

The program has examined the candidates content knowledge and works closely with the Mathematics Department to improve content courses. The faculty closely monitor the students' performance on the exams and are implementing new entrance requirements. They also provide a detailed reflection on candidates' professional and pedagogical skills and impact on student learning. They are planning to implement new courses on classroom management and assessment.

**PART E - AREAS FOR CONSIDERATION**

Areas for consideration

NCTM 2020 Standards for Secondary and Middle Level Mathematics were released in Summer 2020. Documentation can be found at www.nctm.org/caep. Programs should begin transitioning assessments to align with the new standards.

**PART F - ADDITIONAL COMMENTS**

F.1. Comments on Section I (Context) and other topics not covered in Parts B-E:

F.2. Concerns for possible follow-up by the CAEP site visitors:

**PART G - DECISIONS**

Please select final decision:

- **National Recognition.** The program is recognized through the semester and year of the provider's next CAEP accreditation decision in 5-7 years. The Recognition Report will serve as program level evidence for the accreditation cycle it has been initiated. **To retain recognition and to gather new evidence for the next accreditation cycle, another program report must be submitted mid-cycle 3 years in advance of the next scheduled accreditation visit.** The program will be listed as Nationally Recognized through the semester of the next CAEP accreditation decision on websites and/or other publications of the SPA and CAEP. The institution may designate its program as Nationally Recognized by the SPA, through the semester of the next CAEP accreditation decision, in its published materials. **Please note that once a program has been Nationally Recognized, it may not submit another report addressing any unmet standards or other concerns cited in the recognition report.**

Please click "Next"

This is the end of the report. Please click "Next" to proceed.