

**Math 110, Spring 2016**  
**HWK04 due Feb 17**

1. Compute these integrals via substitution.

(a)  $\int_0^4 \sqrt{5y+1} dy$

(b)  $\int \sqrt{\frac{x^4}{x^3-1}} dx$

(c)  $\int_1^{e^{\pi/4}} \frac{4 dt}{t(1+(\ln t)^2)}$

2. Compute these integrals via integration by parts.

(a)  $\int_0^{\ln 2} t^2 e^{4t} dt$

(b)  $\int \arcsin y dy$

(c)  $\int_0^1 x^3 e^{x^2/2} dx$

3. Compute these integrals via any means you can.

(a)  $\int \frac{dx}{x(\ln x)^3}$

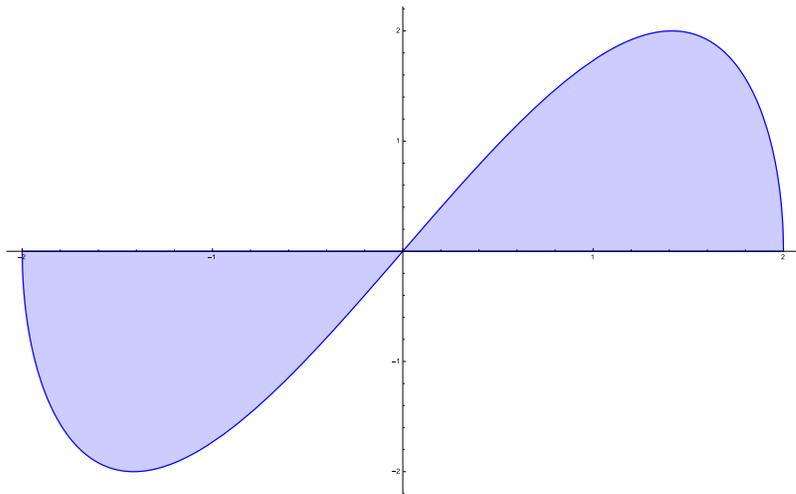
(b)  $\int \frac{\ln x}{x} dx$

(c)  $\int e^x \sin(e^x) dx$

(d)  $\int e^{2x} \sin(x) dx$

(e)  $\int \ln(x + x^2) dx$

4. Find the area of the shaded region. The curved boundary is  $y = x\sqrt{4 - x^2}$  (problem 5.6 #47 in the book).



5. The figure shows triangle AOC inscribed in the region cut from the parabola  $y = x^2$  by the horizontal line  $y = a^2$ . Find the limit as  $a$  approaches zero of the ratio of the area of the triangle to the area of the parabolic region (problem 5.6 #107 in the book).

