Prof. Anchordoqui

Problems set #1

Physics 303

1. A process on an ideal gas is defined by $P = AT^{b}$. (i) Express this process in terms of (P, V) and (V, T). (ii) Calculate compressibility and thermal expansivity in this process. (iii) What is the limitation on b? (iv) For which values of b this process becomes a known process? (v) Find adiabatic values of the two thermodynamic coefficients above.

2. A process on an ideal gas is defined by $P = AT^2$, with A = constant. Calculate the received work and heat upon changing the temperature from T_1 to T_2 . Assume $C_V = \text{constant}$.

3. System A is in equilibrium and has $V_A = 2 \text{ m}^3$ and $P_A = 0.01$ bar. System B is in equilibrium, and has $V_B = 3 \text{ m}^3$ and $P_B = 0.02$ bar. Systems A and B are put in thermal contact with each other, and it is found that they are also in thermal equilibrium with each other. Suppose that the densities of each system are very dilute. Moreover, suppose that the gas in each system happens to be N₂0 (nitrous oxide). Throughout in what follows, suppose that the systems remain closed, i.e. they do not leak or exchange gasses. (i) Compute the ratio M_A/M_B of the masses of the gas in each container. (ii) System A is kept in contact with system B. The volume V_A is slowly changed to $V'_A = 4 \text{ m}^3$, and the pressure P_A is changed to $P'_A = 0.03$ bar. The volume V_B is unchanged, $V'_B = 3 \text{ m}^3$. What should the new pressure P'_B be, in order for the systems A and B to remain in thermal equilibrium? (iii) Is the temperature of the systems, in their final state of part (ii), hotter or colder than they were in their initial state? Compute the ratio $T_{\text{final}}/T_{\text{initial}}$, where the temperatures are measured in Kelvin.

4. A tank of volume 10 m³ contains nitrous oxide at a pressure 1000 Pa and temperature of 20° C. Assume that it behaves like an ideal gas. (i) How many kilomoles of N₂O are in the tank? (ii) How many kilograms? (iii) Find the pressure if the temperature is increased to 50° C. (iv) At a temperature of 20°C, how many kilomoles should be withdrawn from the tank for the pressure to become 100 Pa?

5. A glass bottle of nominal capacity 250 cm³ is filled brim full of water at 20° C. If the bottle and contents are heated to 50° C, how much water spills over? (For water, $\beta = 0.21 \times 10^{-3} \text{ K}^{-1}$. Assume that the expansion of the glass is negligible.)

6. Calculate the heat capacity in the process $P = AT^b$ of an ideal gas, expressing it as a function of T. Analyze different cases of b.