

5. The nucleus of ${}^8\text{Be}$, which consists of 4 protons and 4 neutrons, is very unstable and spontaneously breaks into two alpha particles (helium nuclei, each consisting of 2 protons and 2 neutrons). (i) What is the force between the two alpha particles when they are 5.00×10^{-15} m apart, and (ii) what will be the magnitude of the acceleration of the alpha particles due to this force? Note that the mass of an alpha particle is $4.0026 u$.

Solution (i) Since the charges have opposite signs, the force is repulsive. The magnitude of the force is given by Coulombs law, $F = \frac{1}{4\pi\epsilon_0} \frac{4e^2}{r^2} = 8.99 \times 10^9 \frac{\text{Nm}^2}{\text{C}^2} \frac{4(1.6 \times 10^{-19} \text{ C})^2}{(5.00 \times 10^{-15} \text{ m})^2} = 36.8 \text{ N}$. (ii) The mass of an alpha particle is $m = 4.0026 u$, where $u = 1.66 \times 10^{-27} \text{ kg}$ is the unified mass unit. Applying Newton's 2nd law, the acceleration of either alpha particle is then $a = \frac{F}{m} = \frac{36.8 \text{ N}}{4.0026 \cdot 1.66 \times 10^{-27} \text{ kg}} = 5.54 \times 10^{27} \text{ m/s}^2$. Of course from Newton's 3rd law, both alpha particles experience the same force, and hence undergo the same acceleration.