

## What is Science

Science has a two-fold definition
A body knowledge
A process of learning about nature

Mathematics is a tool for science
Analyze, test and quantify theories

## Scientific theory

## Begins with a hypothesis

$>$ Tries to describe and predict the natural world
$>$ Explain Observations/experiments

- Possibly contributing to or encompassing physical laws


## But theories may break down

$>$ May not be able to explain new observations/ experiments
$>$ A new hypothesis is then proposed to modify or replace current explanations

- Must also be under observational/experimental scrutiny


## Occam's Razor

$>$ When there exist two competing theories that make exactly same prediction, the simpler one is the better
$>$ A scientific theory should be
$\checkmark$ simple
$\checkmark$ without fewest unproven assumptions
$\checkmark$ verificable

# An Harly Scientific Question 

Is the Sun or the Farth at the center of our universe?
$>$ The answer is neither

- but which view best explains the motions of
the stars, planets, and Sun in our sky?
$>$ How this question was tackled over the years gives insight as to how science is performed
- also gives a historical context to astronomy

Farly Astronomy and Planetary Motion Aristotle

- Farth is a sphere that is positioned at center of theuniverse
- Geocentric cosmology


## Aristarchus

- Sun is at center of the universe
- Sun and stars are stationary
- Farth and planets revolve around the sun

In contemporary Greece, Aristotle was far more influential than Aristarchus

- the Farth-centered universe became the accepted norm Observational evidence:
- Farth is not felt to move beneath ones feet, so it must be stationary
- Stars, planets, and Sun seem to revolve around the Farth


## Claudius Ptolemy

## $90 \mathrm{AD}-168 \mathrm{AD}$



## Ptolemaic Model

## Claudius Ptolemaeus

Devised a Geocentric model to describe motion of heavenly bodies
Based on teachings of Aristotle and other Greek scholars

Motion of celestial objects must have perfect uniform circular motion

Hxplained observed retrograde motion of the planets


## Retrograde motion



## Retrograde motion



## Retrograde motion



## Retrograde motion



## Retrograde motion



## Retrograde motion



## Retrograde motion



## Retrograde motion



## 9

## Retrograde motion of Mars



Object seems to reverse its general direction with respect to background stars

Hxample w Path of Mars

# Retrograde motion A Geocentric Explanation 


$>$ In order to account for retrograde motion Ptolemaic model incorporates epicycles

- تpicycle orbits on a circle called the deferent
- Planet moves along epicycle


## Retrograde motion A Geocentric Explanation


> Ptolemaic model reasonably explains retrograde motion
$>$ Further predictions of planetary positions using Ptolemaic model did not match observations

## Retrograde motion A Geocentric Explanation


> Ptolemaic model reasonably explains retrograde motion
$>$ Further predictions of planetary positions using Ptolemaic model did not match observations

## Retrograde motion A Geocentric Explanation


> Ptolemaic model reasonably explains retrograde motion
$>$ Further predictions of planetary positions using Ptolemaic model did not match observations

## Retrograde motion A Geocentric Explanation


> Ptolemaic model reasonably explains retrograde motion
$>$ Further predictions of planetary positions using Ptolemaic model did not match observations

## Retrograde motion A Geocentric Explanation


> Ptolemaic model reasonably explains retrograde motion
$>$ Further predictions of planetary positions using Ptolemaic model did not match observations

## Retrograde motion A Geocentric Explanation


$>$ Ptolemaic model reasonably explains retrograde motion
$>$ Further predictions of planetary positions using Ptolemaic model did not match observations

## Retrograde motion A Geocentric Explanation


$>$ Ptolemaic model reasonably explains retrograde motion
$>$ Further predictions of planetary positions using Ptolemaic model did not match observations

## Retrograde motion A Geocentric Explanation


> Ptolemaic model reasonably explains retrograde motion
$>$ Further predictions of planetary positions using Ptolemaic model did not match observations

## Retrograde motion A Geocentric Explanation


> Ptolemaic model reasonably explains retrograde motion
$>$ Further predictions of planetary positions using Ptolemaic model did not match observations

## Retrograde motion A Geocentric Explanation


> Ptolemaic model reasonably explains retrograde motion
$>$ Further predictions of planetary positions using Ptolemaic model did not match observations

## Retrograde motion A Geocentric Explanation


$>$ Ptolemaic model reasonably explains retrograde motion
$>$ Further predictions of planetary positions using Ptolemaic model did not match observations

## Retrograde motion A Geocentric Explanation


$>$ Ptolemaic model reasonably explains retrograde motion
$>$ Further predictions of planetary positions using Ptolemaic model did not match observations


## Placing the Sun at the Center

Ideas of Aristarchus were revived
$\checkmark$ heliocentric cosmology

Planets, including Farth, orbit the Sun

Hasily explains complex motions of the planets

## Copernican Model

- Devised a heliocentric model of universe
© Sun is the center, and planets revolved around it in perfect circles
- Correctly placed the position of the known planets of the time Mercury, Venus, Farth, Mars, Jupiter, Saturn
- The Moon orbits the Farth
- Stars are fixed
- Hlegantly describes retrograde motion
- Hrror is introduced due to assumption that orbits are perfect circles



## Retrograde motion

## A Heliocentric Explanation



Hxplained due to Farth being closer to Sun than Mars and orbiting more rapidly 1-4 w Mars appears to move eastward with respect to background stars 4-6 w Farth passes Mars-Mars seems to reverse direction 6-9 w تarth passed Mars-Mars resumes eastward motion

## Planetary Configurations



## Inferior planets (Mercury, Venus)

Inferior conjunction: Planet in line with Sun \&e Farth on same side of Sun as Farth Superior conjunction: Planet in line with Sun \&e Farth on opposite side of Sun to Farth Hlongation: Planet makes 90 degree angle between Sun and Farth

## Planetary Configurations



Superior planets (Mars, Jupiter, Saturn, Uranus, Neptune)
Conjunction: Planet in line with Sun \&e Farth on opposite side of Sun to Farth Opposition: Planet in line with Sun \&e Farth on same side of Sun as Farth

Heliocêntrico


Geocêntrico


Heliocêntrico


Heliocêntrico
Geocêntrico


Heliocêntrico


Heliocêntrico


Heliocêntrico


Heliocêntrico


Heliocêntrico


Geocêntrico


Heliocêntrico
Geocêntrico


Heliocêntrico


Heliocêntrico


## Synodic and sidereal periods



|  | Synodic <br> (year) | Sidereal <br> (year) |
| :--- | :---: | :---: |
| Mercury | 0.318 | 0.241 |
| Venus | 1.599 | 0.616 |
| Earth | - | 1.0 |
| Mars | 2.136 | 1.9 |
| Jupiter | 1.092 | 11.9 |
| Saturn | 1.035 | 29.5 |
| Uranus | 1.013 | 84.0 |
| Neptune | 1.008 | 164.8 |

## SynodicYear

~ time between consecutive conjunctions of planet with Harth

## Sidereal Year

w time for that planet to make one full rotation around Sun with respect to background stars

## Tycho Brahe (1546-1601)



## Tycho's cosmos

Tycho had made most accurate observations obtained at that time on planets

Tycho's model of heavens had planets orbiting around Sun and Sun orbiting around Earth at center of the Universe


## Johannes Kepler (1571-1630)



## Kepler's Laws



Defined by Johannes Kepler

- Using Tycho's observations

Assumption planetary orbits are circular introduces errors when making predictions

Invoking elliptical orbits provides a far better description

## Geometric Aside

## Hlliptical \#ccentricity


$>$ Fccentricity measures the deviation of a circle
$>$ As eccentricity e increases the shape elongates

$>$ aphelion distance - distance farthest from Sun
$>$ perihelion distance - distance closest to Sun

## Geometry of ellipses



## Kepler's First Law



The orbit of a planet around the Sun is an ellipse, with the Sun at one focus

## Kepler's First Law



Focus 1 Sun

Focus 2 -
Empty

## Kepler's First Law



Focus 1 Sun

Focus 2 -
Empty

## Kepler's First Law



Focus 1 Sun

Focus 2 Empty

## Kepler's First Law



Focus 1 -
Sun

Focus 2 -
Empty

## Kepler's First Law



Focus 1 Sun

Focus 2 Empty

## Kepler's First Law



Focus 1 Sun

Focus 2 Empty

## Kepler's First Law



Focus 1 Sun

Focus 2 -
Empty

## Kepler's Second Law



## A line joining a planet and Sun sweeps out equal areas in equal intervals of time


 -


 <br> <br> } <br> \section*{Kepler's Second Law <br> \section*{Kepler's Second Law <br> <br> 29} <br> <br> 29}

$$
\square
$$ -


.



#### Abstract


F

( .
$\qquad$
 Coser


O O , O  $\square$ $\qquad$
$\qquad$ <br> anepier s Deconc LevN
}


#### Abstract




（
震
R

$$
\square
$$

－ － 0 ．




\author{

## IEpler＇s Second Iaw

}

\author{

## IEpler＇s Second Iaw

}
 $+$

 $\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

（


\begin{abstract}


#### Abstract

．


\end{abstract}



星
－ n ， O
 $\log$ $+$



，




－
－
－


－ －
－
－
 Tor
 $\square$

正
 －

## 2r

Kepler＇s Second Law AGPLLS SGCOLC LEWW


． ．

  正

IEDIOR's Second Law
.
IEpler's Second Iaw
 ．

\section*{IEPDer＇s Second Law <br> 


（GPLED＇S

Kepler＇s Second Law ，




$$
1
$$

## （e） <br>  <br>  <br> ． <br> ． <br>  

}
，
.
位
㕍

$$
-
$$

f

$$
0
$$









#### Abstract




$\qquad$
$\qquad$
$\qquad$


## Kepler＇s Second Law <br> Kepler＇s Second Law <br> \section*{$$
5
$$

}. － ．


， － $+$

震


－
－
$\bullet$ $\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
年 （2） （2nern ． （2nern

$\qquad$
 O


1
 （2nern （2nern ． －

－ （2nern （2nern $\square$为
 $\square$ ， O

 <br> IKeplers s second IeN <br> \section*{\title{
Kepler's Second Law <br> \section*{\title{
Kepler's Second Law <br> <br> <br> Kepler's Second Law
}} <br> <br> <br> Kepler's Second Law
}}

## -







## Kepler's Third Law



The square of a planet's sidereal period around the Sun is directly proportional to the cube of the length of its orbit's semimajor axis

$$
\left(T^{2} \propto R^{3}\right)
$$

## Galileo Galilei (1564-1642)



## Galileo Galilei

$>$ Made many discoveries that supported heliocentric view and Kepler's laws
$>$ Was the first to make use of and published results using a telescope
> Discovered moons of Jupiter
> Discovered that Venus has phases

## Galileo Observations of Venus


$>$ Venus appears small at gibbous phase and large at crescent phase

- Note: Ptolemaic model does not predict Gibbous nor Full phases
$>d$ is diameter in units of arcsec
- the farther an object is the smaller its angular size


## Phases of Venus

© In the Ptolemaic system (left), Venus always lies between the Sun and the Harth and it would always show a crescent phase

- The Copernican system (right) predicts a full range of phases for Venus as it passes from between the Sun and the Farth to being on the opposite side of the Sun from the Farth

$>$ Because of orbital mechanics, a planet with a superior orbit (one that orbits the Sun further away than Earth) will not go through phases, as we see it, because the planet won't cast a shadow from our perspective
$>$ Earth will go through phases from the point of view of any planet that has an orbit superior to earth
$>$ This extends to the relative position of any planet
> Somebody on Jupiter would see phases on Mars, but not on Saturn
> Somebody on Neptune could see phases on all seven of the other planets
$>$ Mars is a partial exception to the superior orbit rule
$>$ You will not see phases on Mars from Mars' shadow of sunlight, but Mars is close enough to Earth that Earth's shadow can cause some partial phasing
> This can make Mars appear irregular (or gibbous) because of Earth's interference with the light from the sun
> Planets further out into the solar system are too distant for Earth to interfere in this way

May 6, 2018

## Galilean Moons of Jupiter

$>$ Discovered that Jupiter has moons
$>$ Confirmed orbits of moons obey Kepler's laws $\left(T^{2} \propto R^{3}\right)$

What is the motion called when a planet seems to be moving westward in the sky?
A. retrogade
B. parallax
C. reverse parallax

What is the motion called when a planet seems to be moving westward in the sky?

## A. retrogade

B. parallax
C. reverse parallax

In Copernican system, what is shape of planets' orbits?
A. elipse
B. parabola
C. circle

In Copernican system, what is shape of planets' orbits?
A. elipse
B. parabola
C. circle

# On what planet does a "year" last only 88 days? 

A. Mars
B. Mercury
C. Jupiter

# On what planet does a "year" last only 88 days? 

A. Mars
B. Mercury
C. Jupiter

## In what year did Galileo first use an optical telescope to

 study the moon?A. 250 BCE

B. 1611
C. 1945

## In what year did Galileo first use an optical telescope to

 study the moon?A. 250 BCE

B. 1611
C. 1945

Galileo discovered something about Venus with his telescope that shook the old theories.

Which of the following was Galileo's discovery?
A. Venus surface is similar to Farth
B. Venus has phases like the moon
C. Venus has rings

Galileo discovered something about Venus with his telescope that shook the old theories.

Which of the following was Galileo's discovery?
A. Venus surface is similar to झarth
B. Venus has phases like the moon
C. Venus has rings

Heliocentric means around:
A. Sun
B. Barth
C. Moon
D. Jupiter

Heliocentric means around:
A. Sun
B. Farth
C. Moon
D. Jupiter

The greatest distance of a planet from the sun is called what? Is it the planet's:

A. aphelion

B. perihelion
C. helix
D. eccentricity

The greatest distance of a planet from the sun is called what? Is it the planet's:

## A. aphelion

B. perihelion
C. helix
D. eccentricity

According to Kepler's Laws, the cube of the mean distance of a planet from the sun is proportional to the:
A. area that is swept out
B. cube of the period
C. square of the period
D. fourth power of the mean

According to Kepler's Laws, the cube of the mean distance of a planet from the sun is proportional to the:
A. area that is swept out
B. cube of the period
C. square of the period
D. fourth power of the mean

## A. ellipses

B. parabolas
C. hyperbolas
D. squares

## A. ellipses

B. parabolas
C. hyperbolas
D. squares

A. Yes

B. No

## A. Yes

B. No

With a telescope here on Harth, would we ever see Jupiter in a crescent phase?
A. Yes
B. No

With a telescope here on Farth, would we ever see Jupiter in a crescent phase?

A. Yes

B. No

## 61 QUERY 3

(i) Mars is 1.5 AU away from the Sun. What is its orbital period?
(ii) Jupiter's mean orbital radius is 5.2 AU. What is the period of Jupiter's orbit around the Sun?
[AU is the abbreviation for astronomical units, where $1 \mathrm{AU}=1.5 \times 10^{11} \mathrm{~m}$ is the mean Earth-Sun distance]

## QUERY 3

(i) Mars is 1.5 AU away from the Sun. What is its orbital period?
(ii) Jupiter's mean orbital radius is 5.2 AU. What is the period of Jupiter's orbit around the Sun?
[AU is the abbreviation for astronomical units, where $1 \mathrm{AU}=1.5 \times 10^{11} \mathrm{~m}$ is the mean Earth-Sun distance]
Kepler's constant

Kepler's law $\quad R^{3}=K T^{2}$
Since Earth is at 1 AU and it takes 1 year to go around the $\operatorname{Sun}-K=\frac{\mathrm{AU}^{3}}{\mathrm{yr}^{2}}$
(i) Period of Mars is m $T=\sqrt{R^{3} / K}=1.84 \mathrm{yr}$
(ii) Period of Jupiter is $T=\sqrt{R^{3} / K}=11.85 \mathrm{yr}$

## 63 QUERY 4

Earth has an orbital period of 365 days and its mean distance from the Sun is $1.495 \times 10^{8} \mathrm{~km}$. The Pluto's mean distance from the Sun is $5.896 \times 10^{9} \mathrm{~km}$. Using Kepler's third law, calculate Pluto's orbital period in Earth days

## 64 QUERY 4

Earth has an orbital period of 365 days and its mean distance from the Sun is $1.495 \times 10^{8} \mathrm{~km}$. The Pluto's mean distance from the Sun is $5.896 \times 10^{9} \mathrm{~km}$. Using Kepler's third law, calculate Pluto's orbital period in Earth days What we know $T_{E}=365$ days $\quad r_{E}=1.495 \times 10^{8} \mathrm{~km} \quad r_{P}=5.896 \times 10^{9} \mathrm{~km}$

$$
\begin{aligned}
& \left(\frac{T_{E}}{T_{P}}\right)^{2}=\left(\frac{r_{E}}{r_{P}}\right)^{3} \\
& \left(\frac{365 \text { days }}{T_{P}}\right)^{2}=\left(\frac{1.495 \times 10^{8} \mathrm{~km}}{5.896 \times 10^{9} \mathrm{~km}}\right)^{3} \\
& \left(\frac{365 \text { days }}{T_{P}}\right)^{2}=\left(2.54 \times 10^{-2}\right)^{3} \\
& \left(\frac{1.32 \times 10^{5} \text { days }^{2}}{T_{P}^{2}}\right)=1.63 \times 10^{-5} \\
& T_{P}=\sqrt{\frac{1.32 \times 10^{5} \text { days }^{2}}{1.63 \times 10^{-5}}}
\end{aligned}
$$

