

Copernícus, Kepler, and Galíleo Luís Anchordoquí

What is Science

Science has a two-fold definition

1

A body knowledge A process of learning about nature

Mathematics is a tool for science Analyze, test and quantify theories

Scientific theory

- Begins with a hypothesis
- > Tries to describe and predict the natural world
- > Explain observations/experiments
- Possibly contributing to or encompassing physical laws
 - But theories may break down
- > May not be able to explain new observations/ experiments
- > A new hypothesis is then proposed to modify or replace current explanations
- Must also be under observational/experimental scrutiny

Occam's Razor

> When there exist two competing theories that make exactly same prediction, the simpler one is the better

> A scientific theory should be

🗹 simple

without fewest unproven assumptions

verificable

An Early Scientific Question

Is the Sun or the Earth at the center of our universe?

- > The answer is neither
 - but which view best explains the motions of the stars, planets, and Sun in our sky?
- > How this question was tackled over the years gives insight as to how science is performed
 - also gives a historical context to astronomy

Early Astronomy and Planetary Motion Aristotle

- Earth is a sphere that is positioned at center of the universe
- Geocentric cosmology Aristarchus
- Sun is at center of the universe
- Sun and stars are stationary
- Earth and planets revolve around the sun In contemporary Greece, Aristotle was far more influential than Aristarchus
- the Earth-centered universe became the accepted norm
 - **Observational evidence:**
 - Earth is not felt to move beneath ones feet, so it must be stationary
 - Stars, planets, and Sun seem to revolve around the Earth

Claudius Ptolemy 90 AD-168 AD



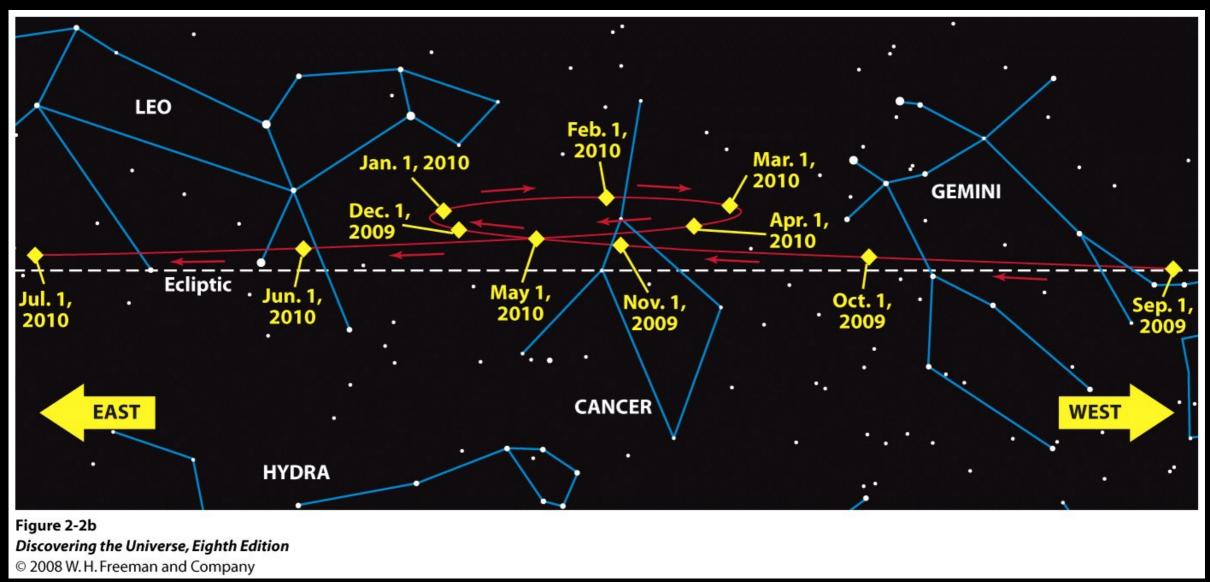
Ptolemaic Model

Claudius Ptolemaeus

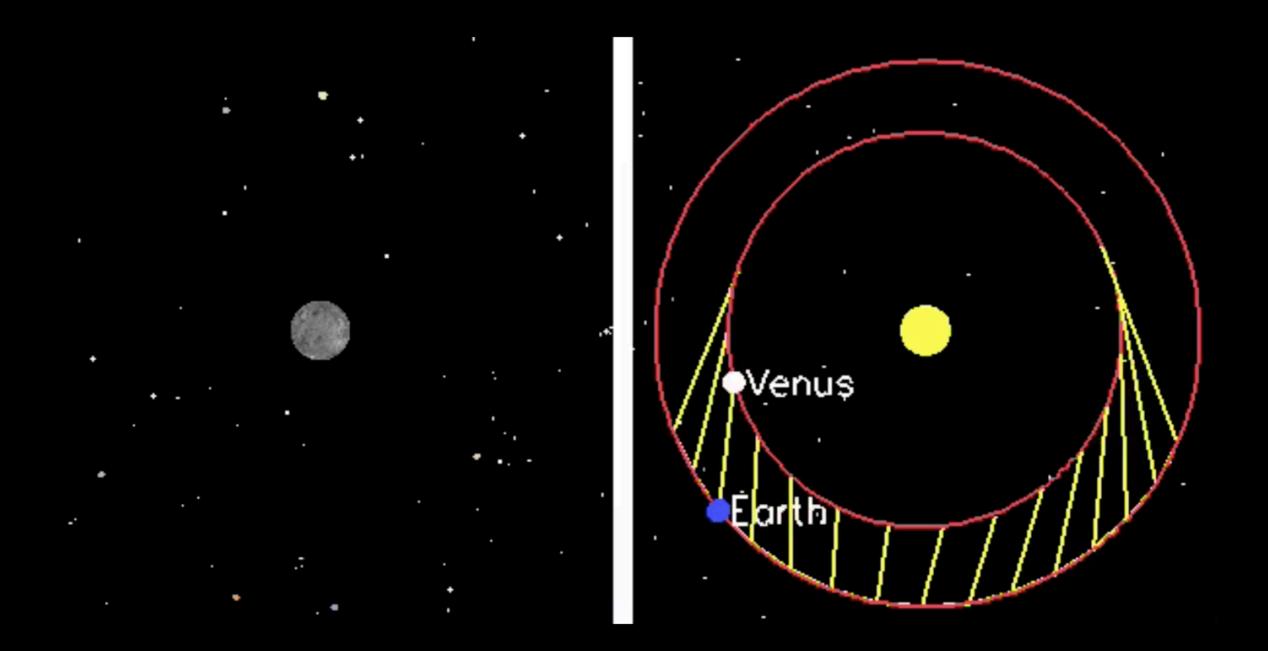
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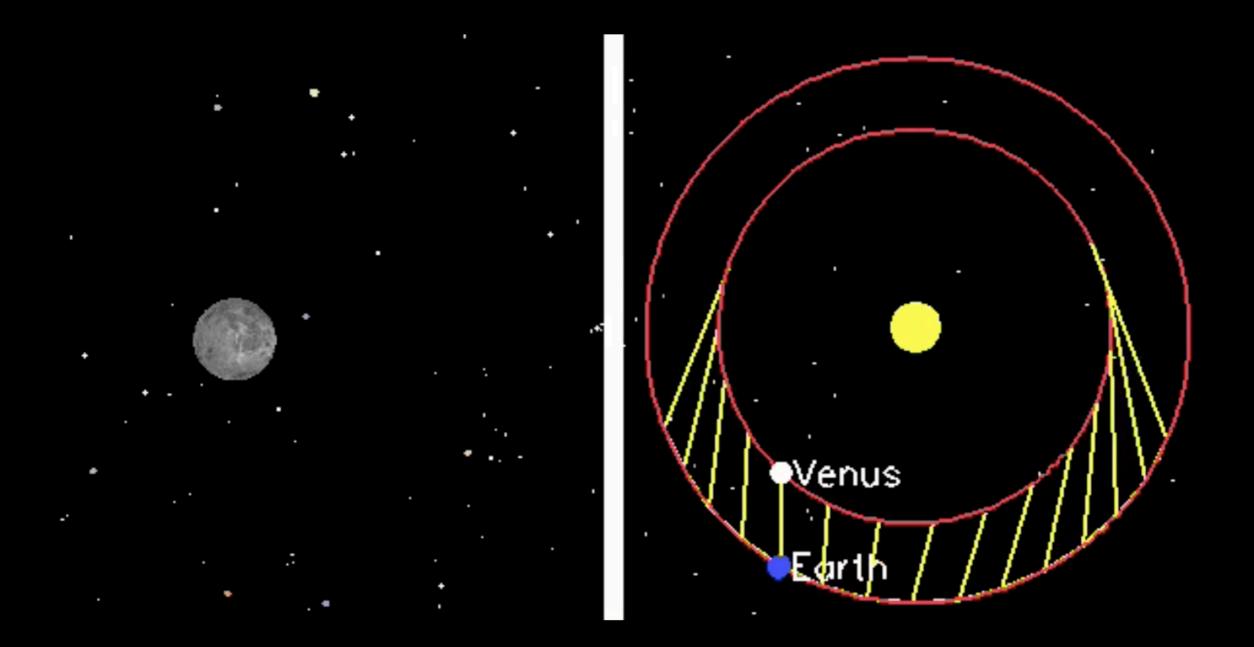
- Devised a Geocentric model to describe motion of heavenly bodies
- Based on teachings of Aristotle and other Greek scholars
- Motion of celestial objects must have perfect uniform circular motion
- Explained observed retrograde motion of the planets

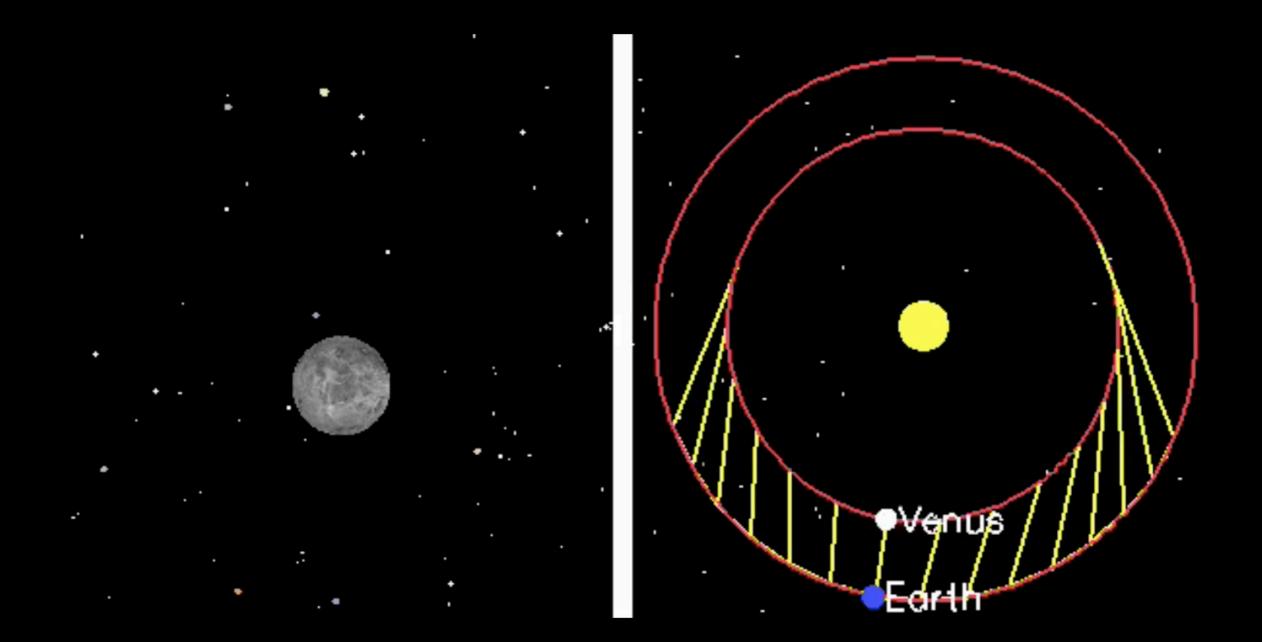


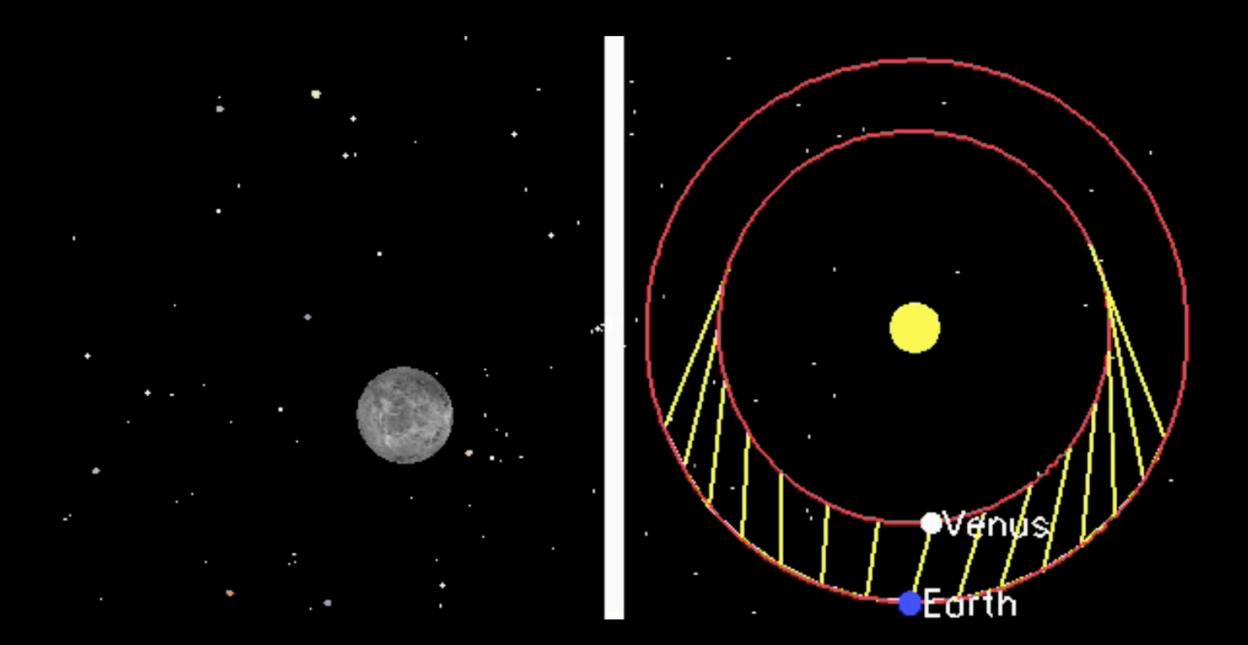


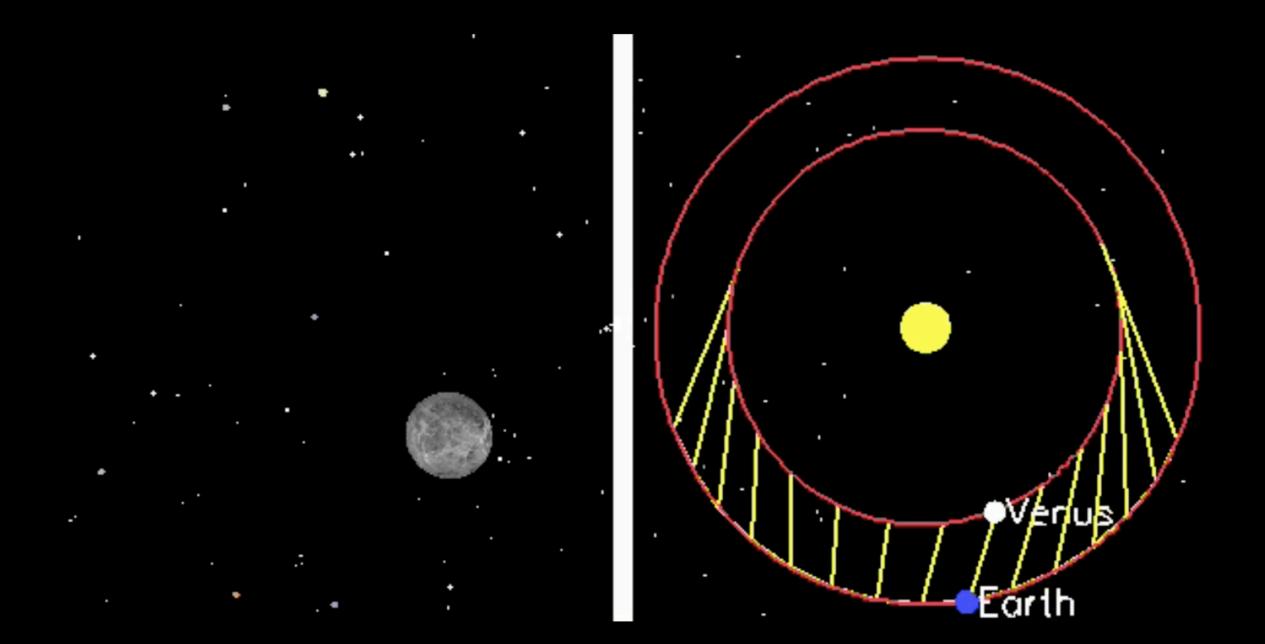
- Object seems to reverse its general direction with respect to the background stars
- Example: Path of Mars

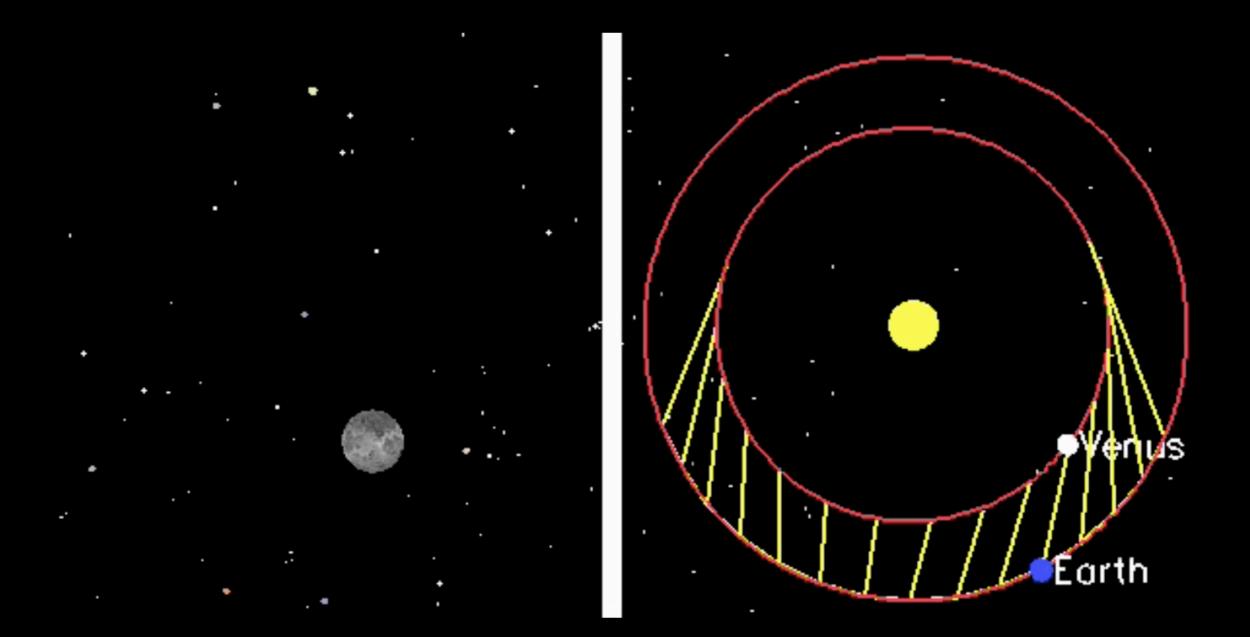


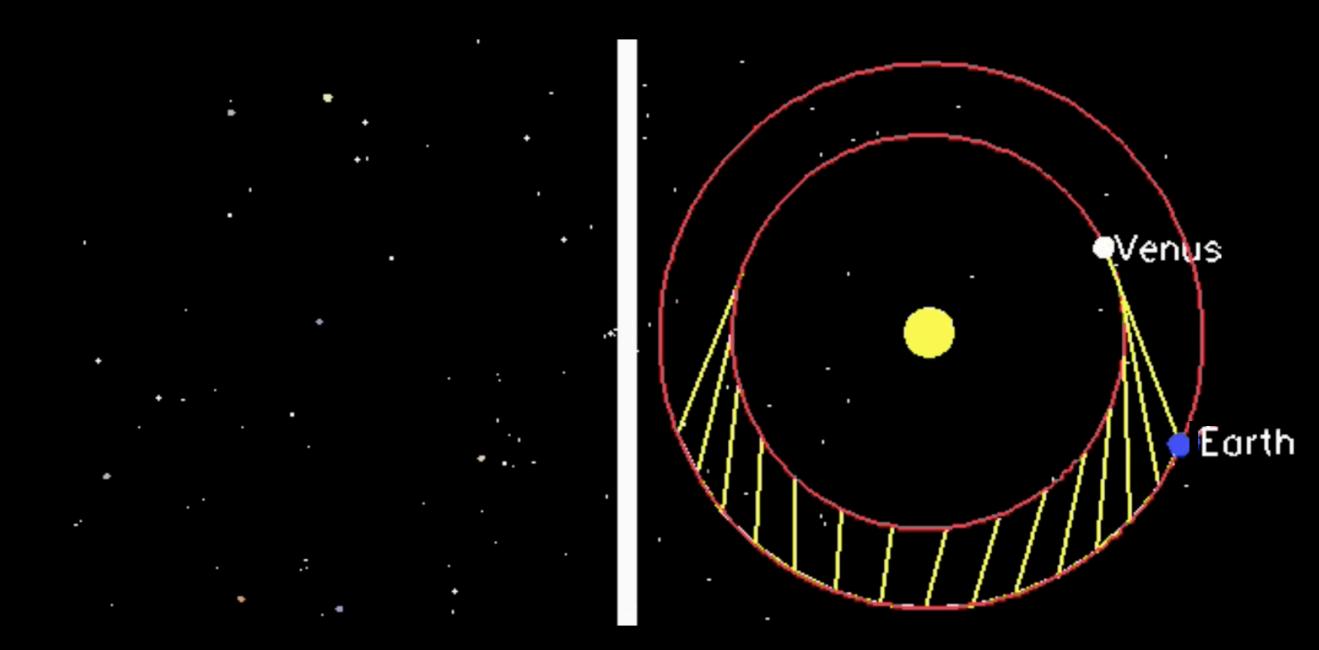




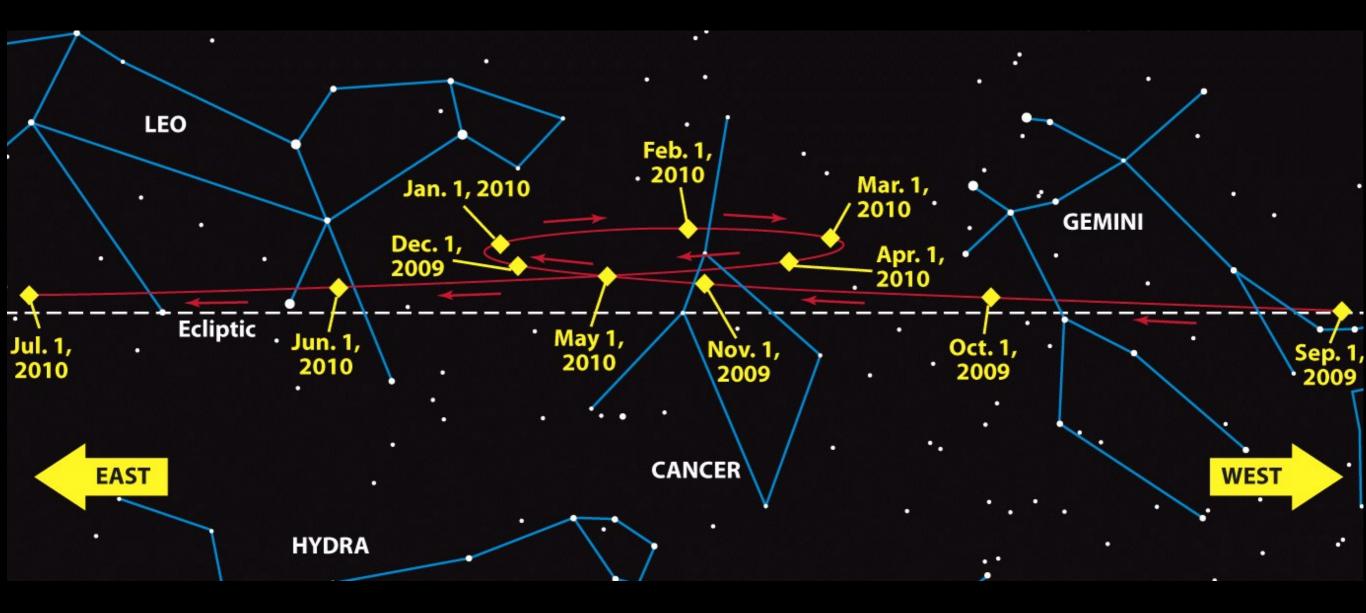








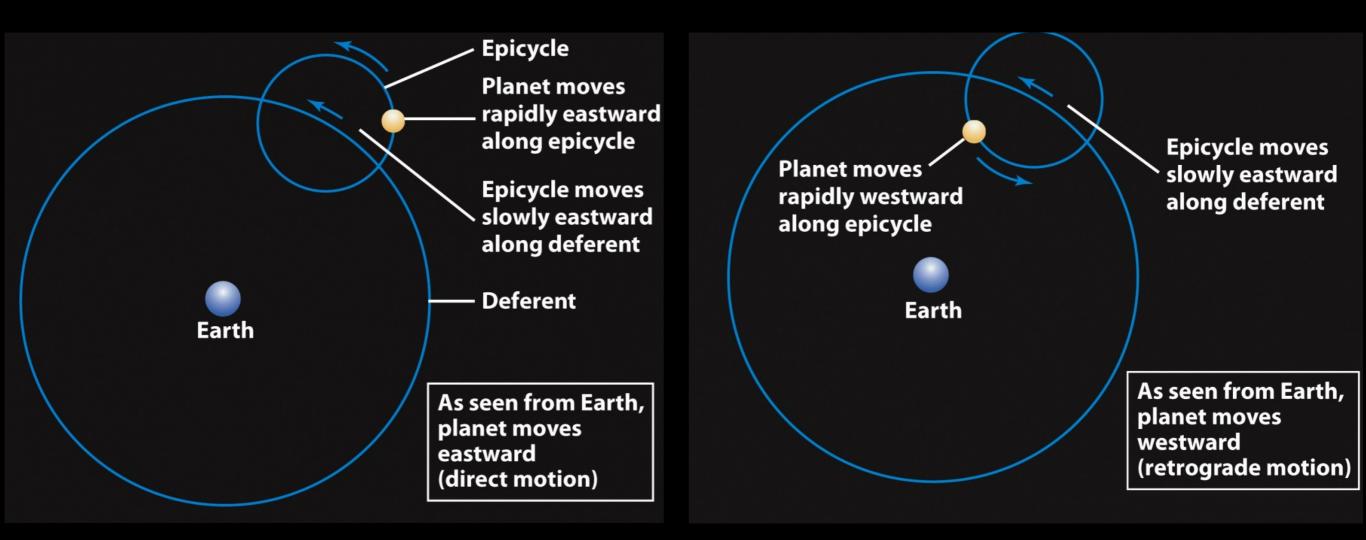
Retrograde motion of Mars



Object seems to reverse its general direction with respect to background stars

Example 🖛 Path of Mars

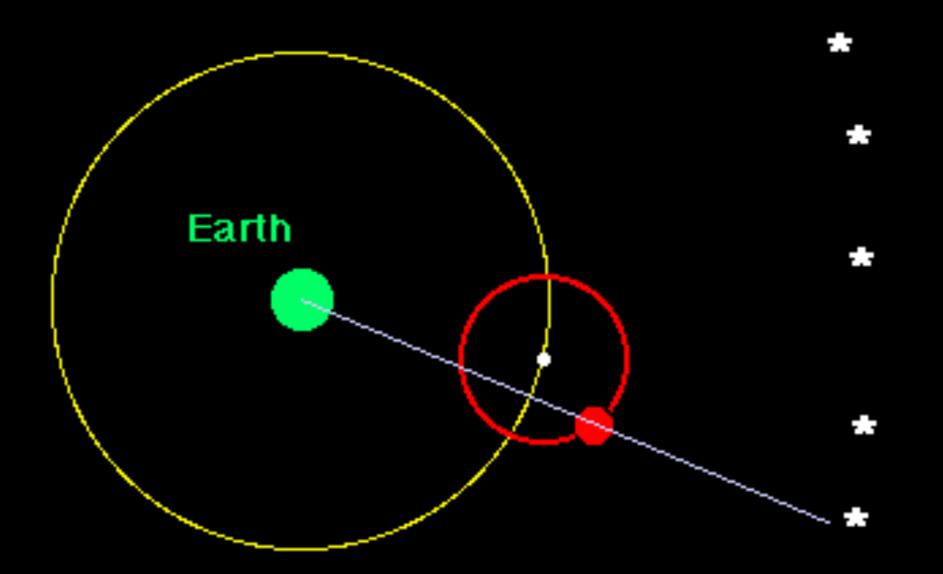
Retrograde motion A Geocentric Explanation



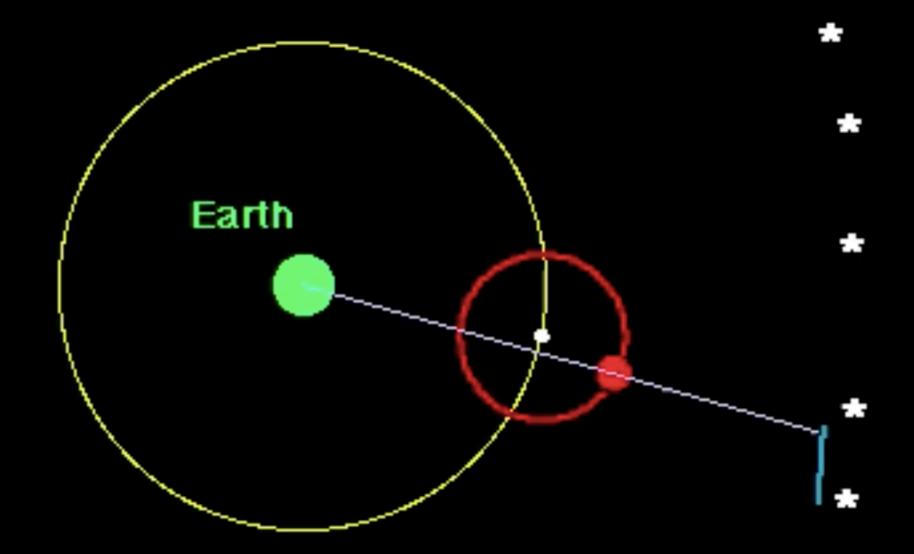
 In order to account for retrograde motion Ptolemaic model incorporates epicycles
 Epicycle orbits on a circle called the deferent
 Planet moves along epicycle

Retrograde motion A Geocentric Explanation

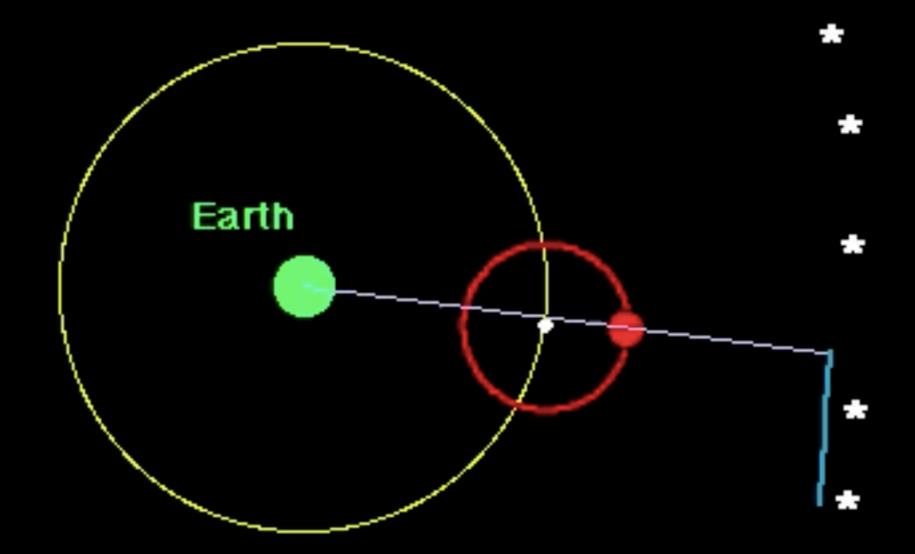
(http://users.clas.ufl.edu/ufhatch/pages/03-sci-rev/sci-rev-home/resource-ref-read/chief-systems/08-0retro-2.htm)



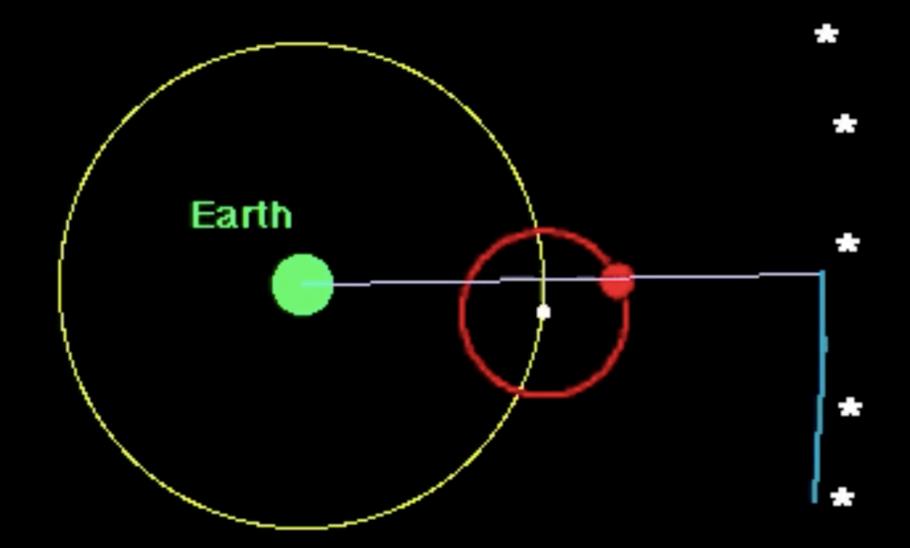
- Ptolemaic model reasonably explains retrograde motion
- Further predictions of planetary positions using the Ptolemaic model did not match observations



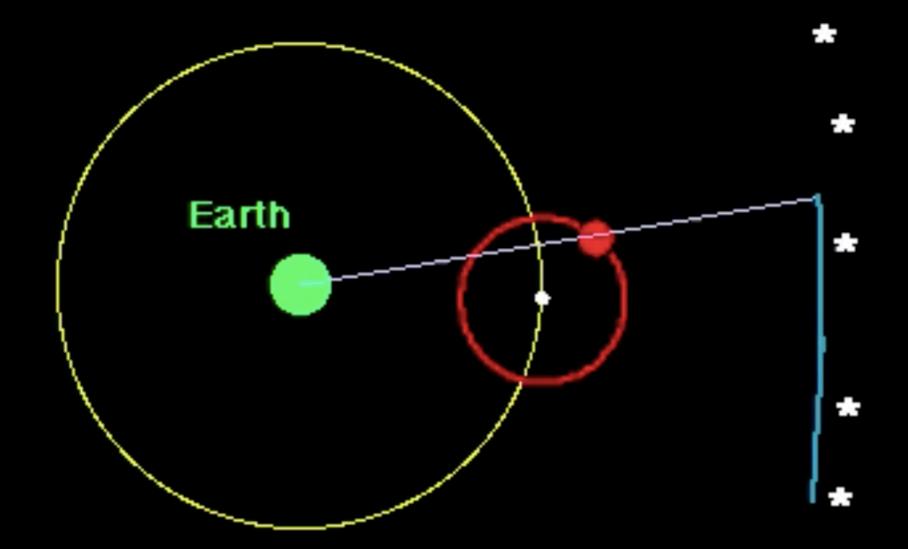
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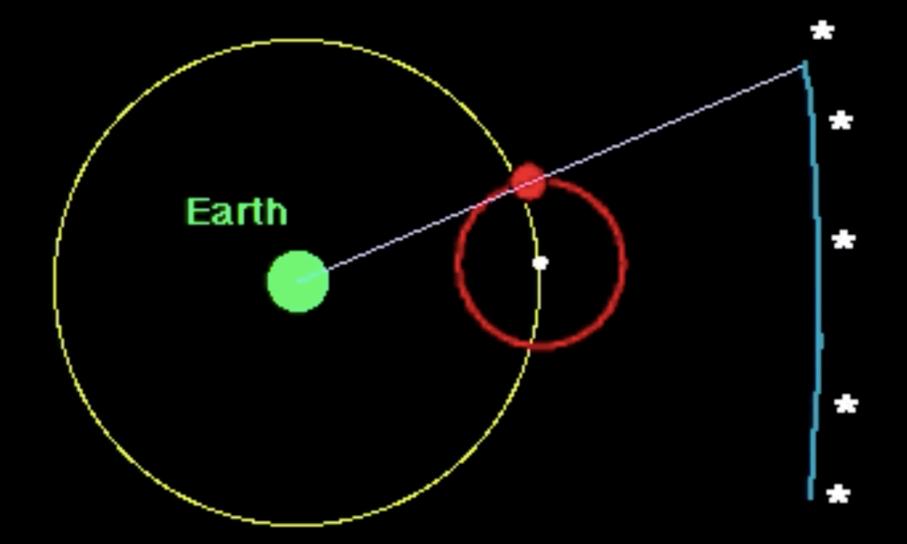
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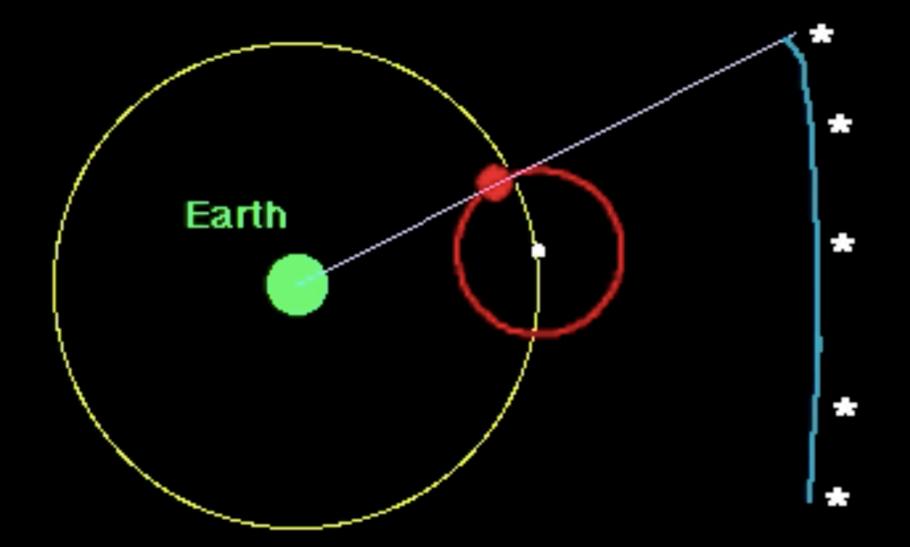
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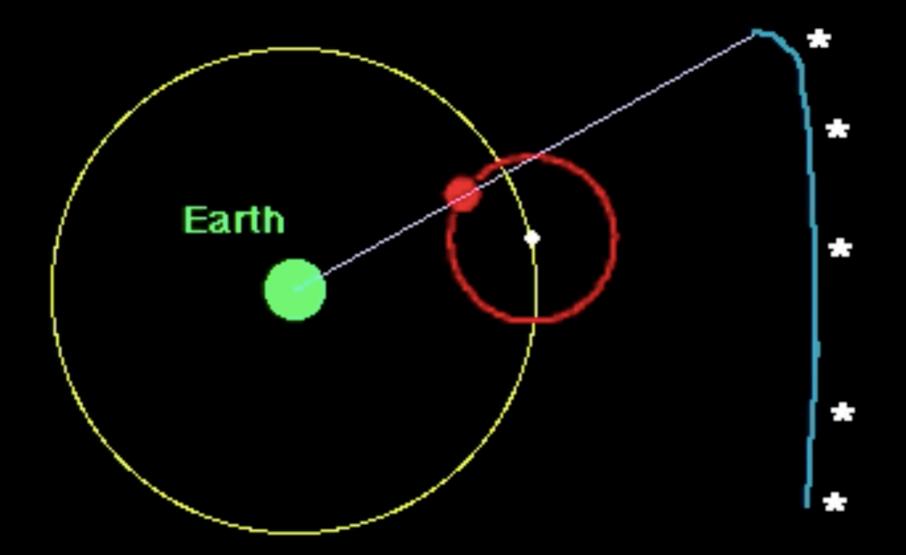
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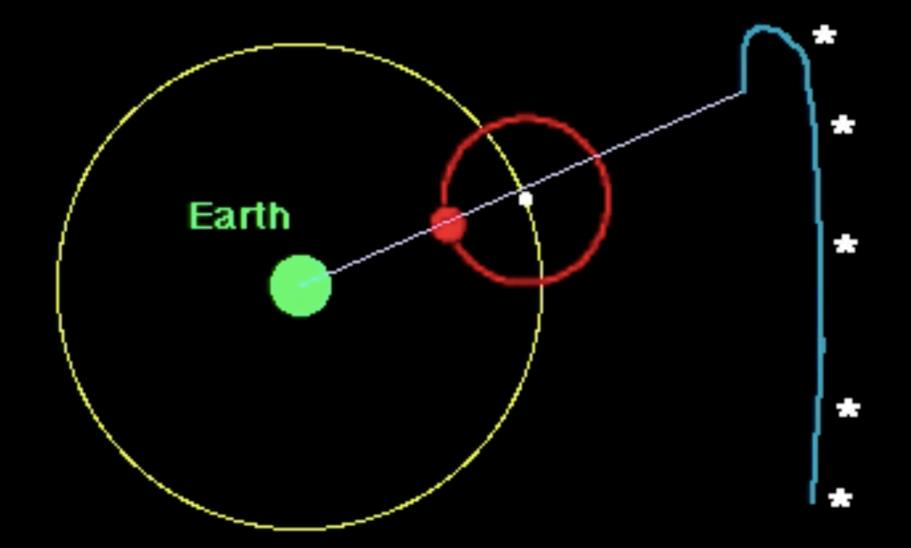
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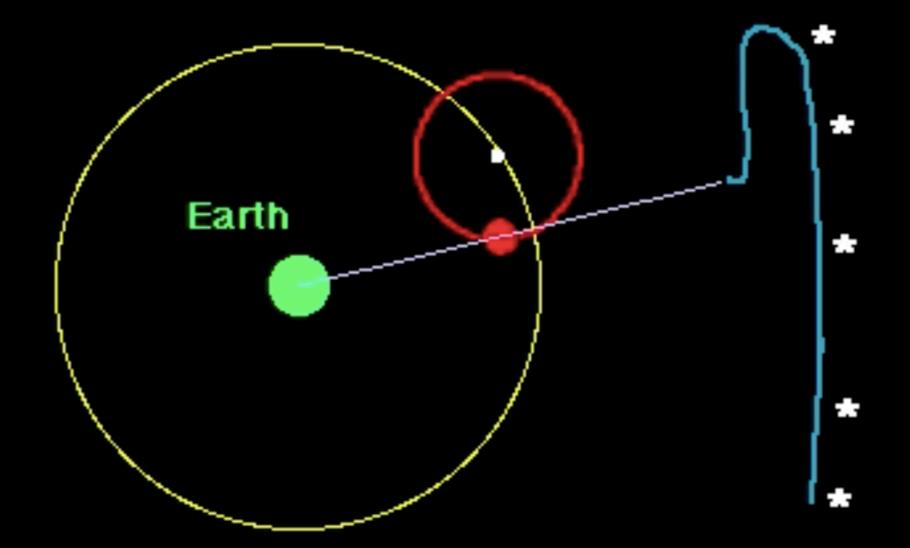
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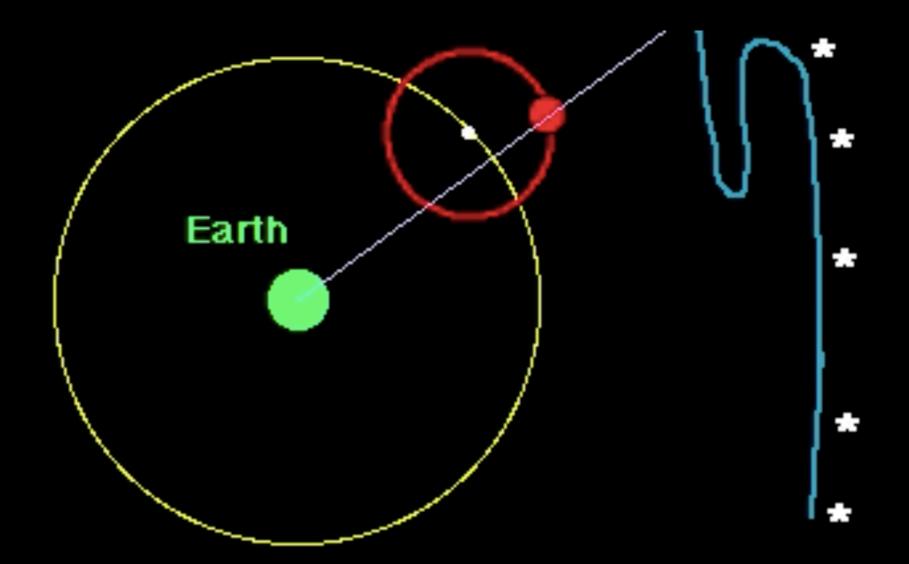


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Retrograde motion A Geocentric Explanation

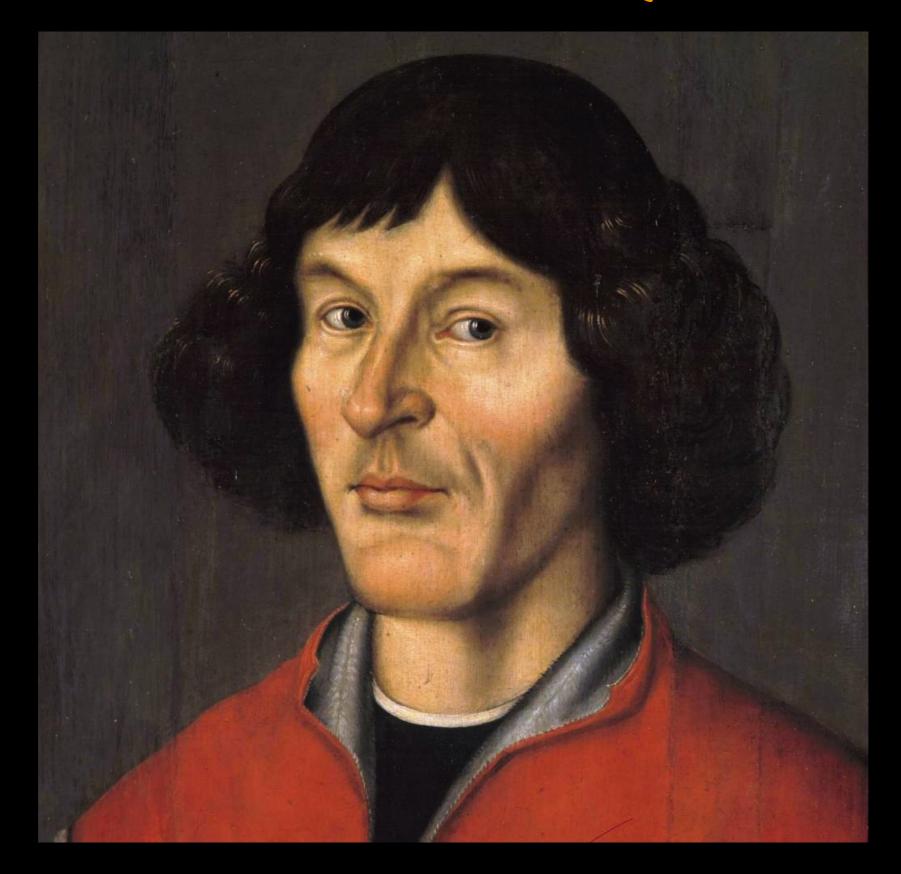
Earth

- > Ptolemaic model reasonably explains retrograde motion
- Further predictions of planetary positions using Ptolemaic model did not match observations



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Niocolaus Copernicus (1473 - 1543)



Placing the Sun at the Center

Ideas of Aristarchus were revived

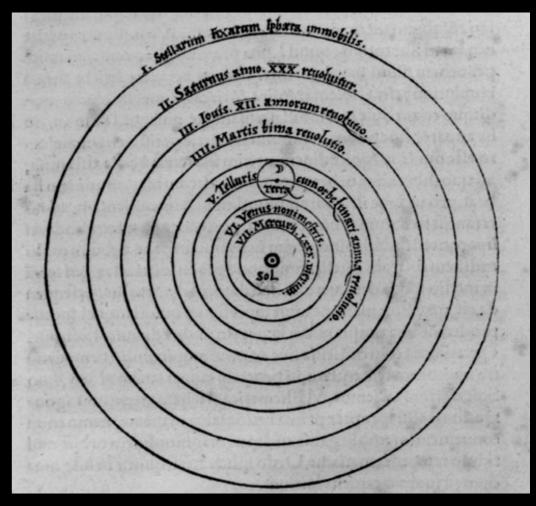
Meliocentric cosmology

Planets, including Earth, orbit the Sun

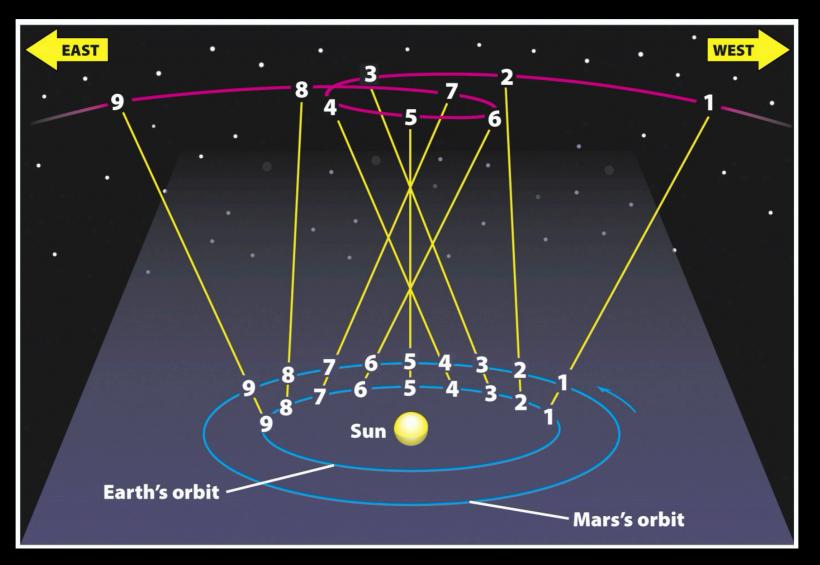
Easily explains complex motions of the planets

Copernican Model

- ② Devised a heliocentric model of universe
- Sun is the center, and planets revolved around it in perfect circles
- Correctly placed the position of the known planets of the time Mercury, Venus, Earth, Mars, Jupiter, Saturn
- The Moon orbits the Earth
- Stars are fixed
- Elegantly describes retrograde motion
- Error is introduced due to assumption
 that orbits are perfect circles



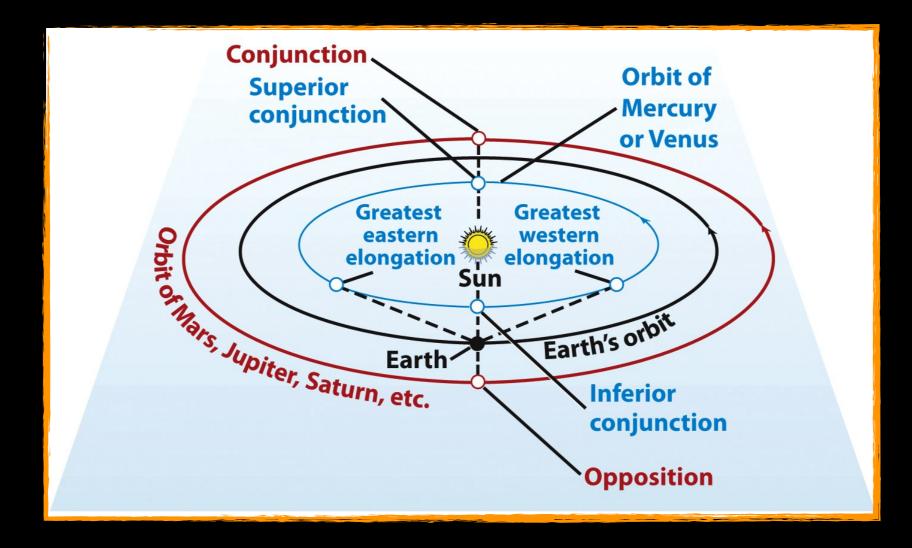
A Heliocentric Explanation



Explained due to Earth being closer to Sun than Mars and orbiting more rapidly

- 1-4 🖛 Mars appears to move eastward with respect to background stars
- 4-6 🖛 Earth passes Mars-Mars seems to reverse direction
- 6-9 🖛 Earth passed Mars-Mars resumes eastward motion

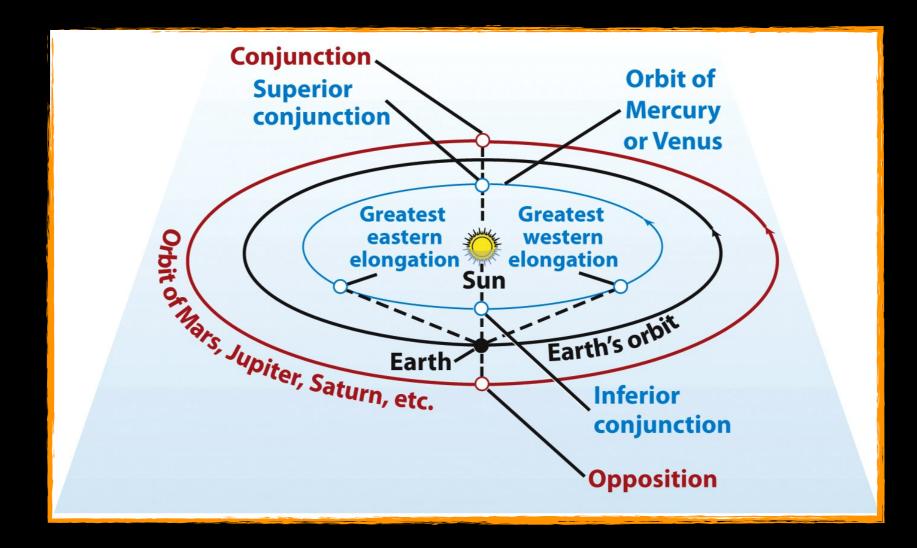
Planetary Configurations



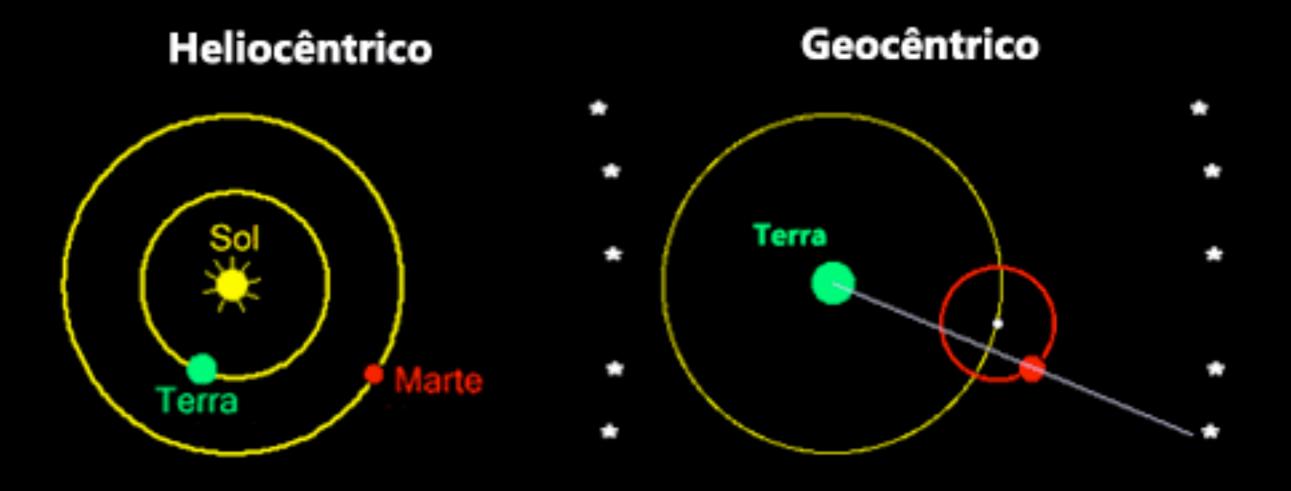
Inferior planets (Mercury, Venus)

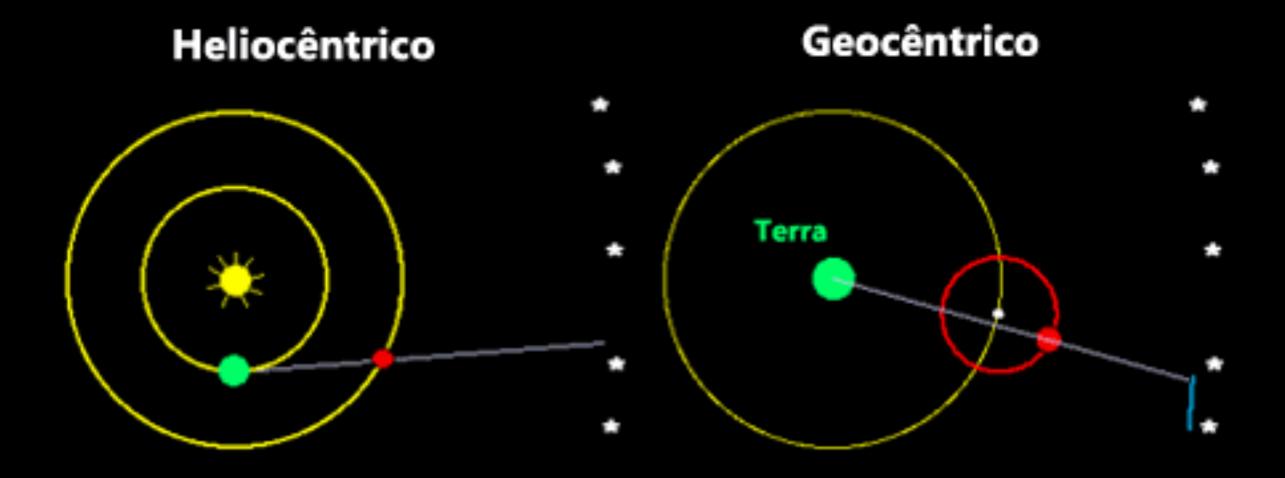
Inferior conjunction: Planet in line with Sun & Earth on same side of Sun as Earth Superior conjunction: Planet in line with Sun & Earth on opposite side of Sun to Earth Elongation: Planet makes 90 degree angle between Sun and Earth

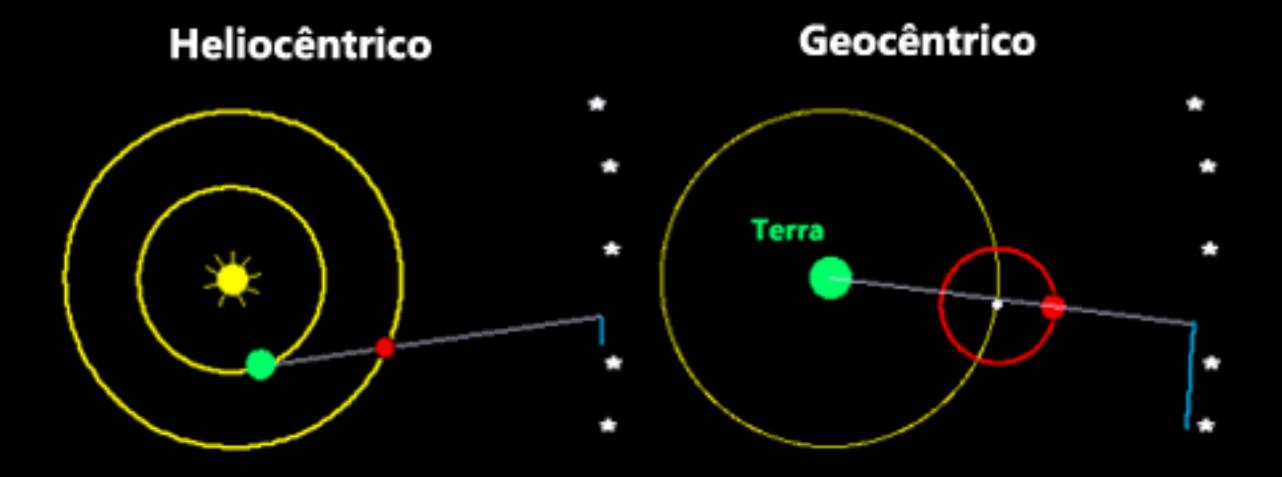
Planetary Configurations

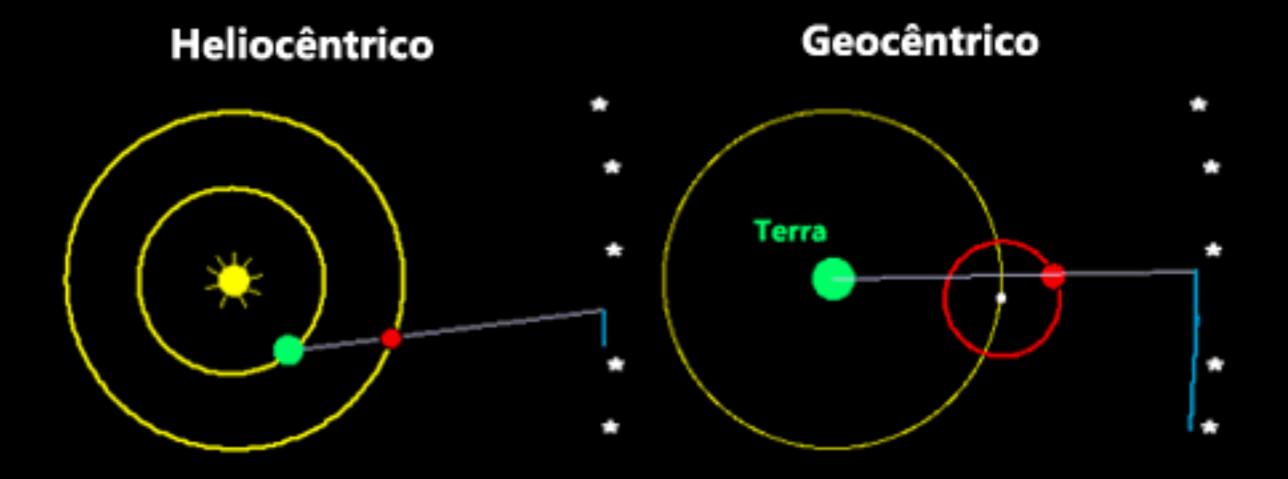


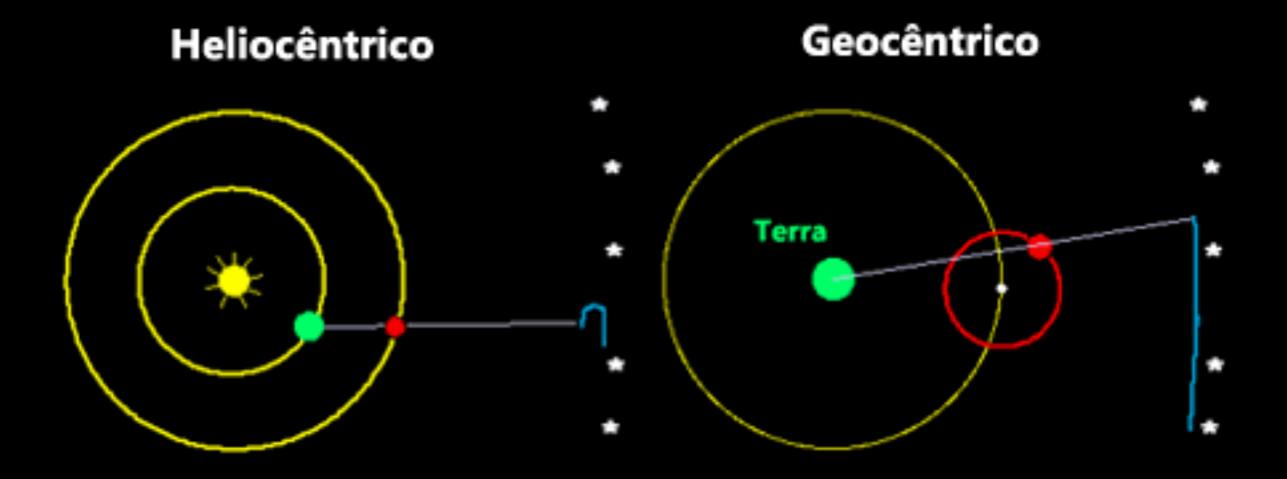
Superior planets (Mars, Jupiter, Saturn, Uranus, Neptune) Conjunction: Planet in line with Sun & Earth on opposite side of Sun to Earth Opposition: Planet in line with Sun & Earth on same side of Sun as Earth

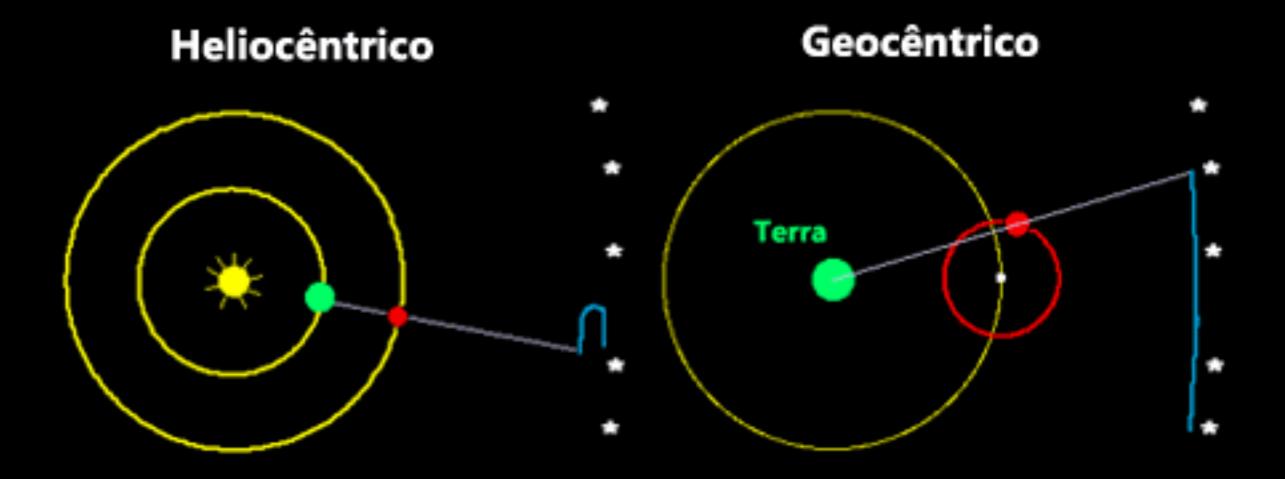


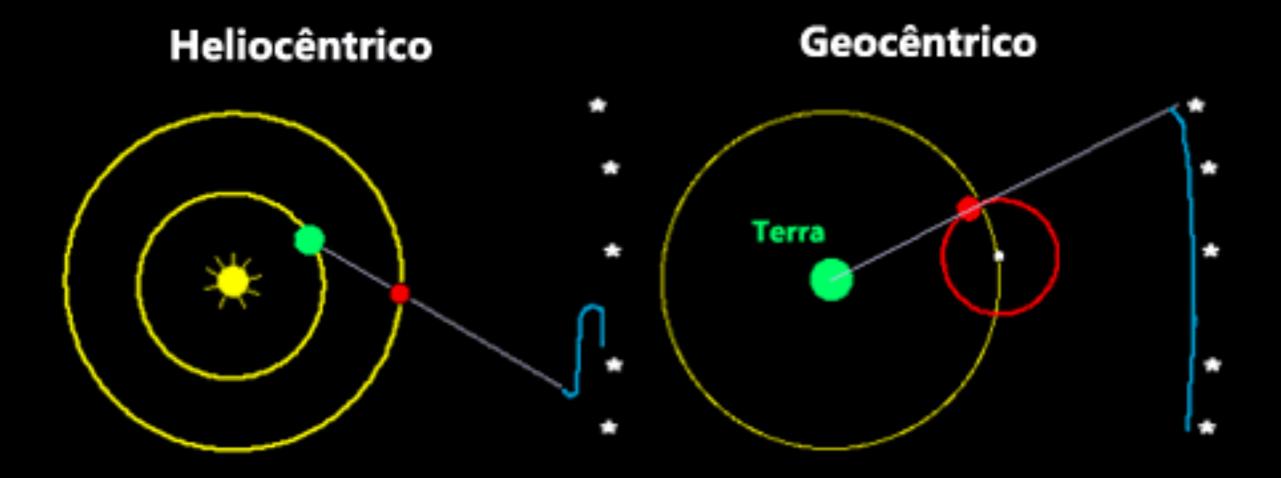


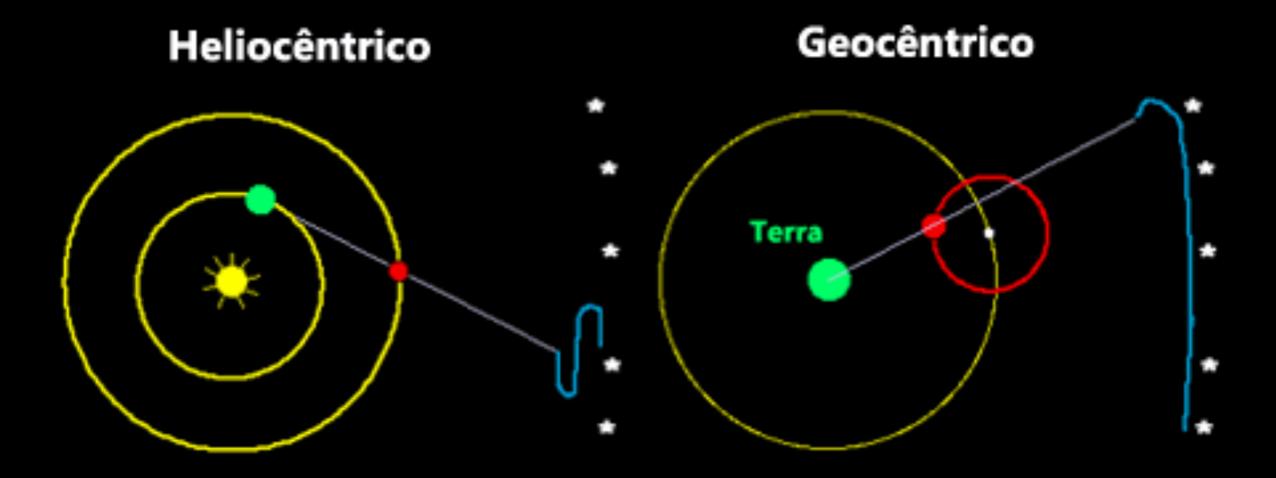


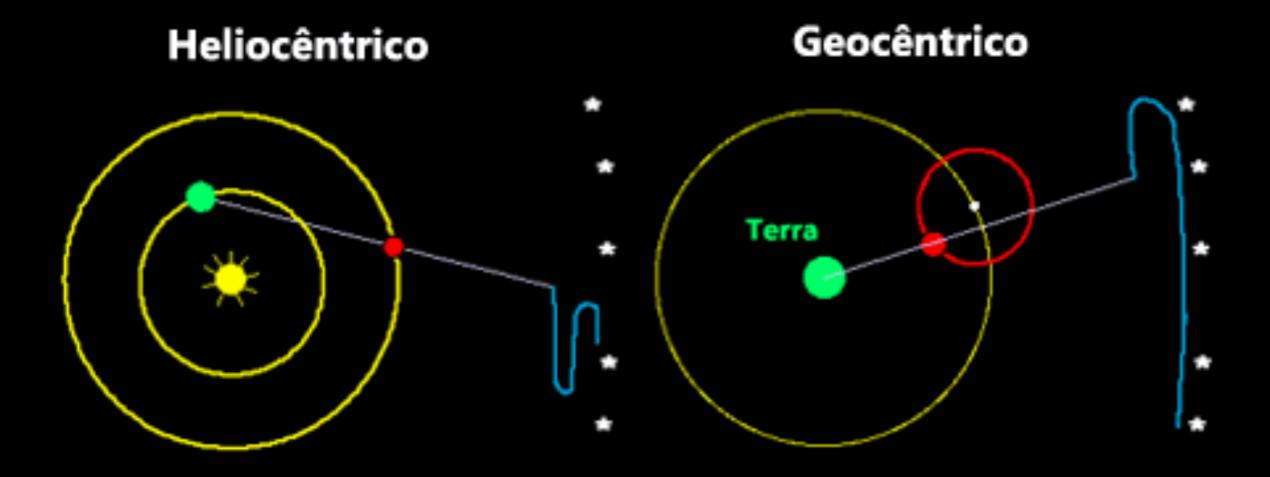


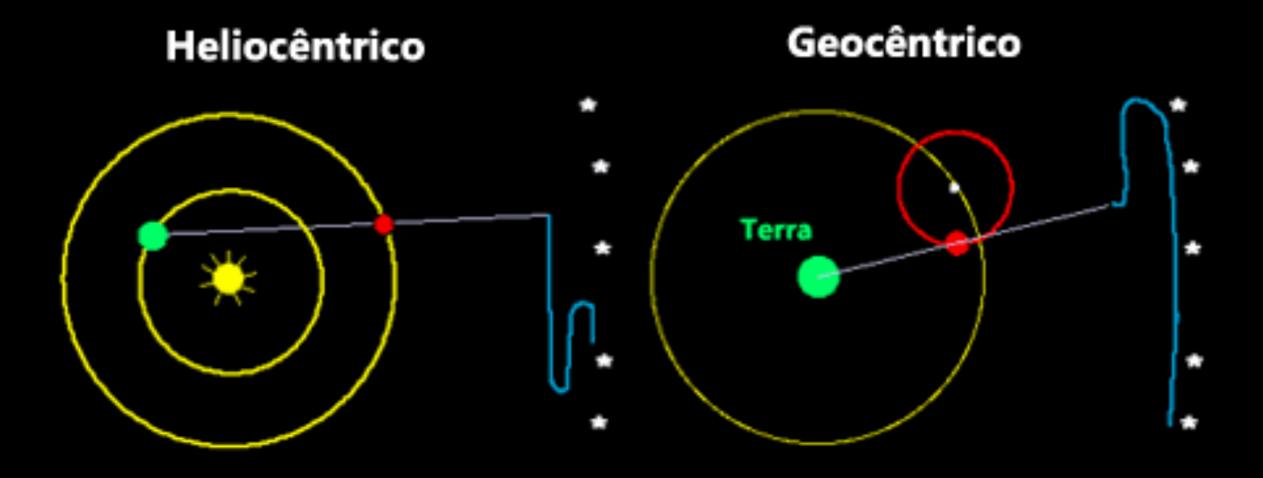


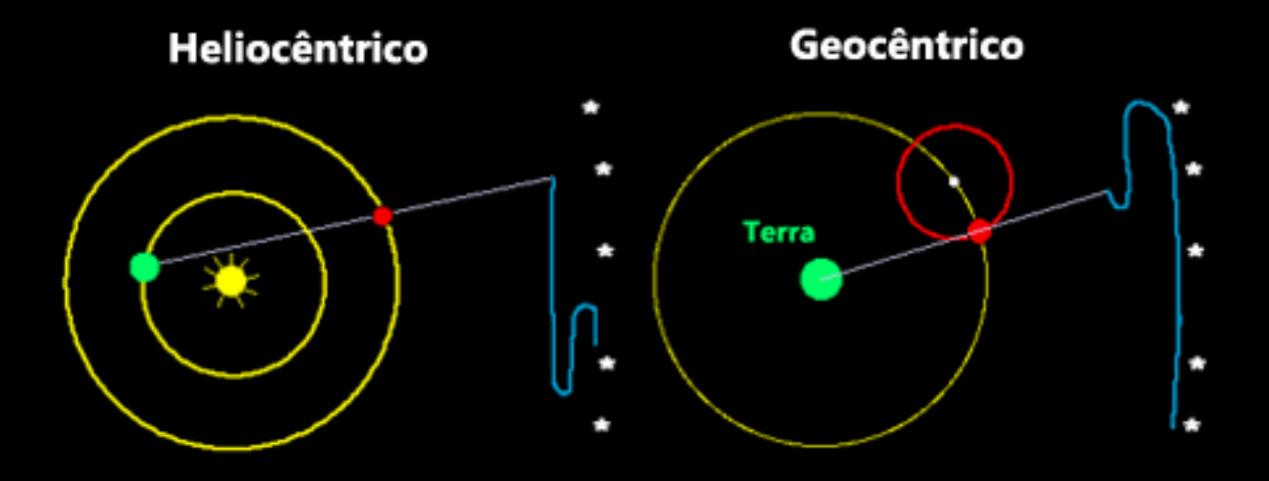


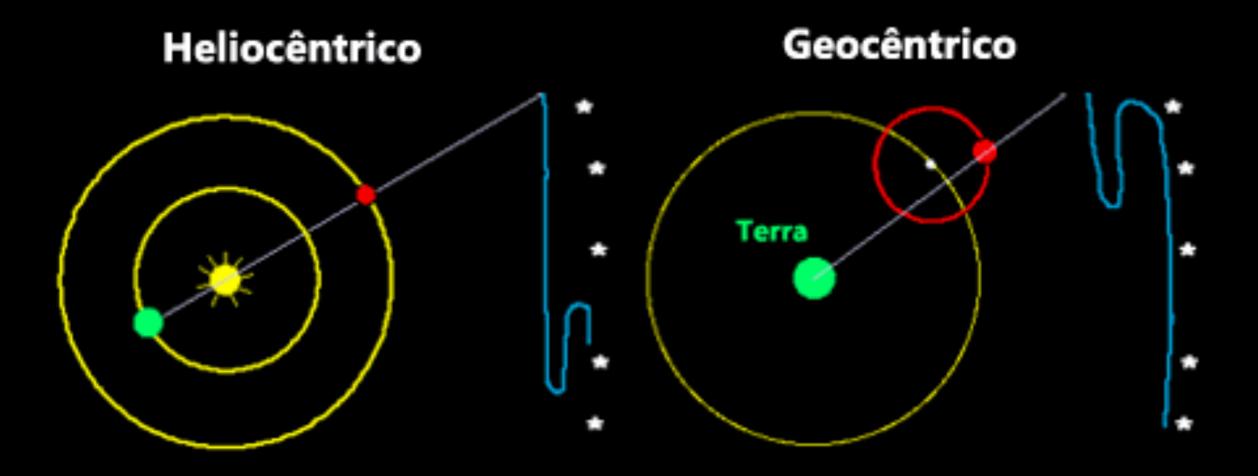






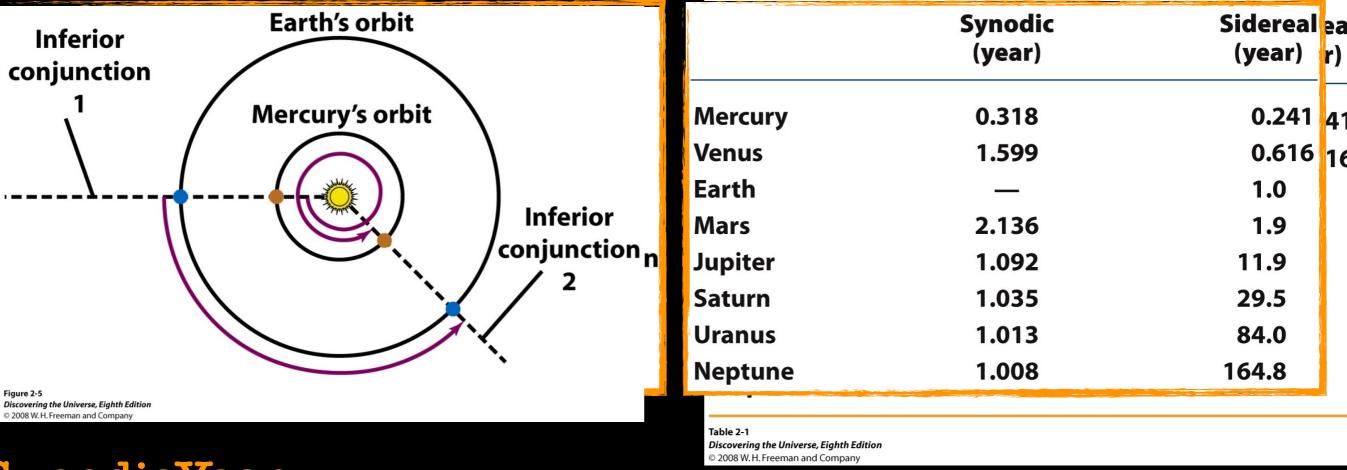






Synodic and sid

TABLE 2-1Synodic and Sidereal Periods of
the Planets (in Earth Years)



SynodicYear

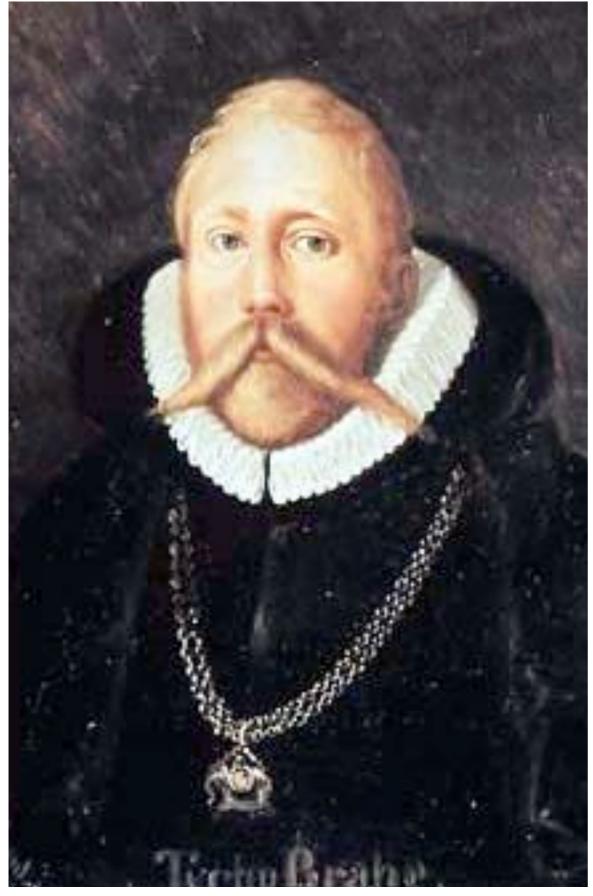
➡ time between consecutive conjunctions of planet with Earth

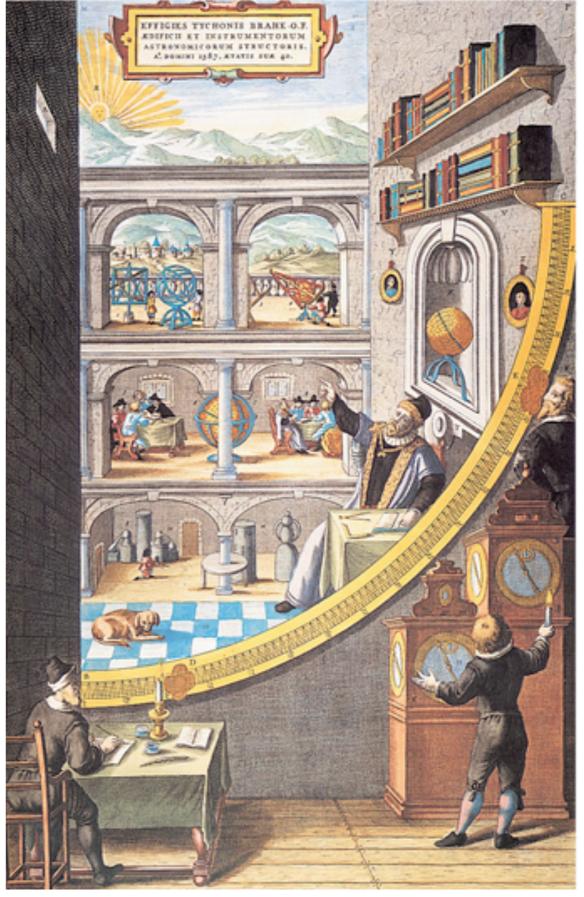
Sidereal Year

time for that planet to make one full rotation around Sun

with respect to background stars

²⁰ Tycho Brahe (1546-1601)



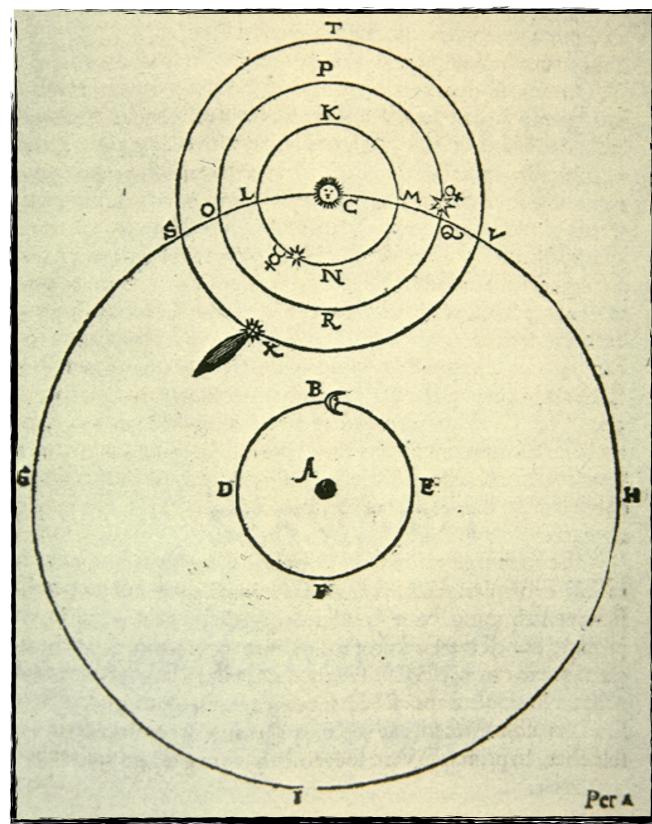


Tydis'cosnos

• Tycho had made the most Tycho had miade most accurate observations obtained at that time on the planets. time on planets Tycho's model of the heavens had the planets orbiting round the Sun Tycho's model of heavens had planets 'orbiting EarthuildhSun and center of the Universe. Sun orbiting around Earth at

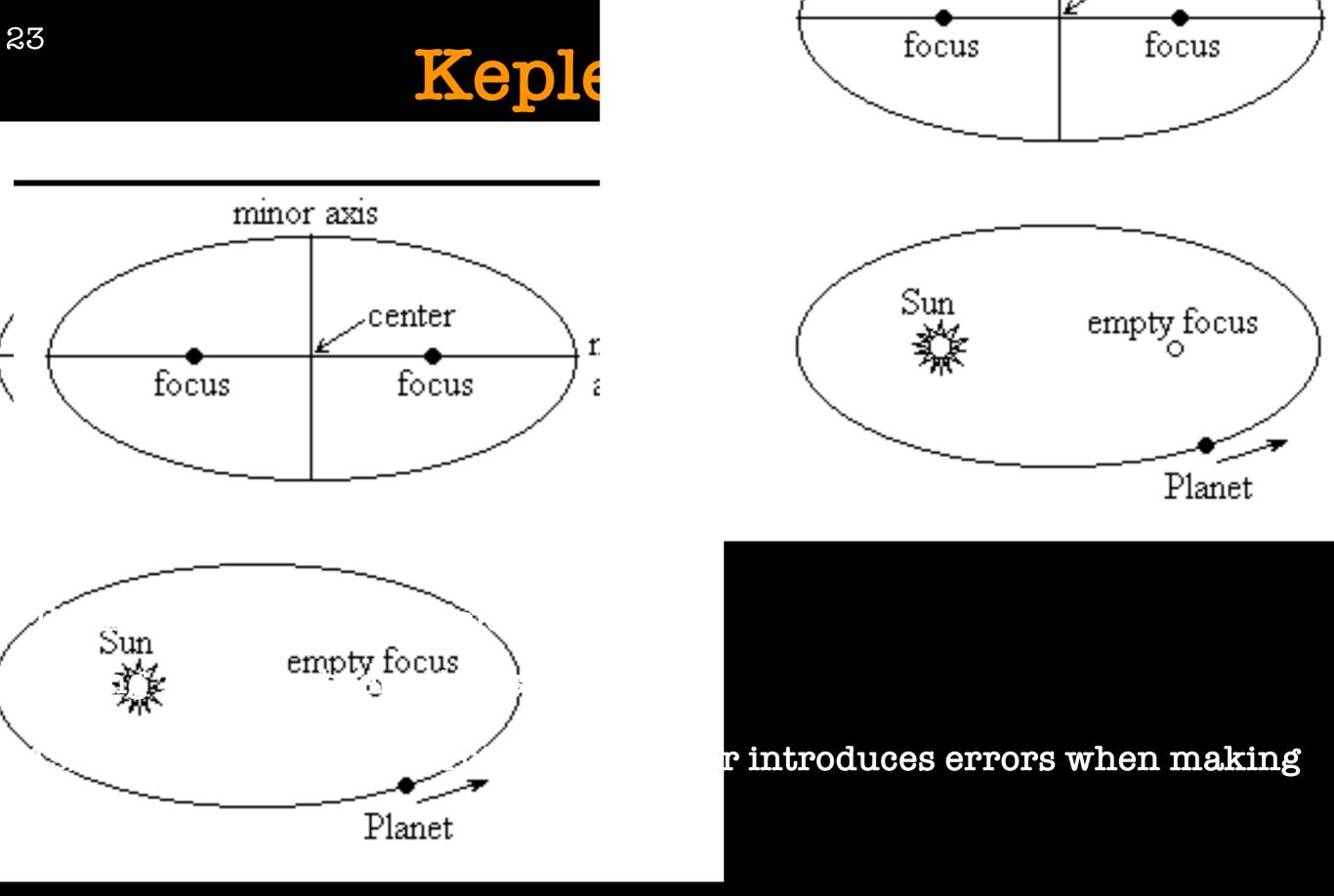
center of the Universe

21



Johannes Kepler (1571-1630)

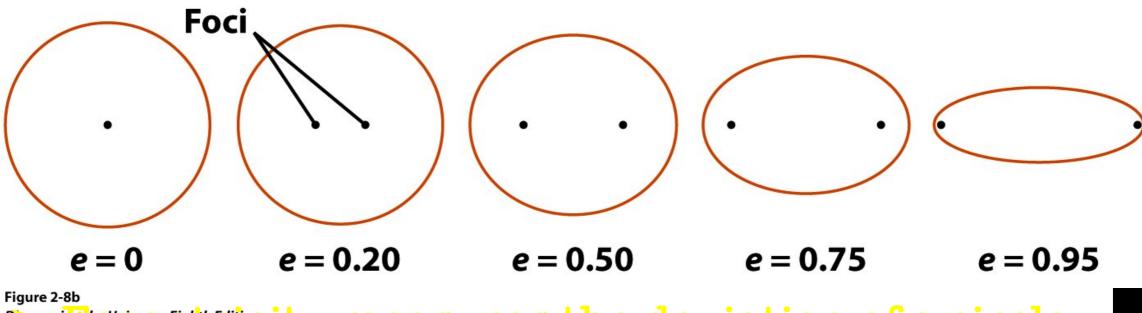




Invoking elliptical orbits provides a far better description

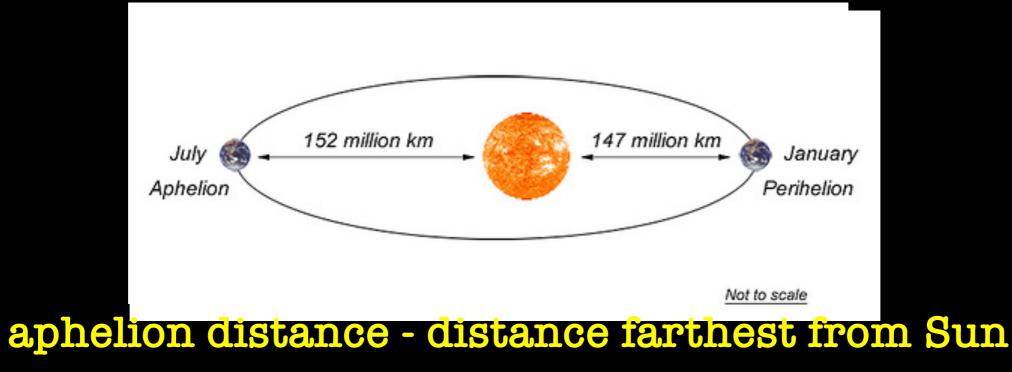
Geometric Aside

Elliptical Eccentricity



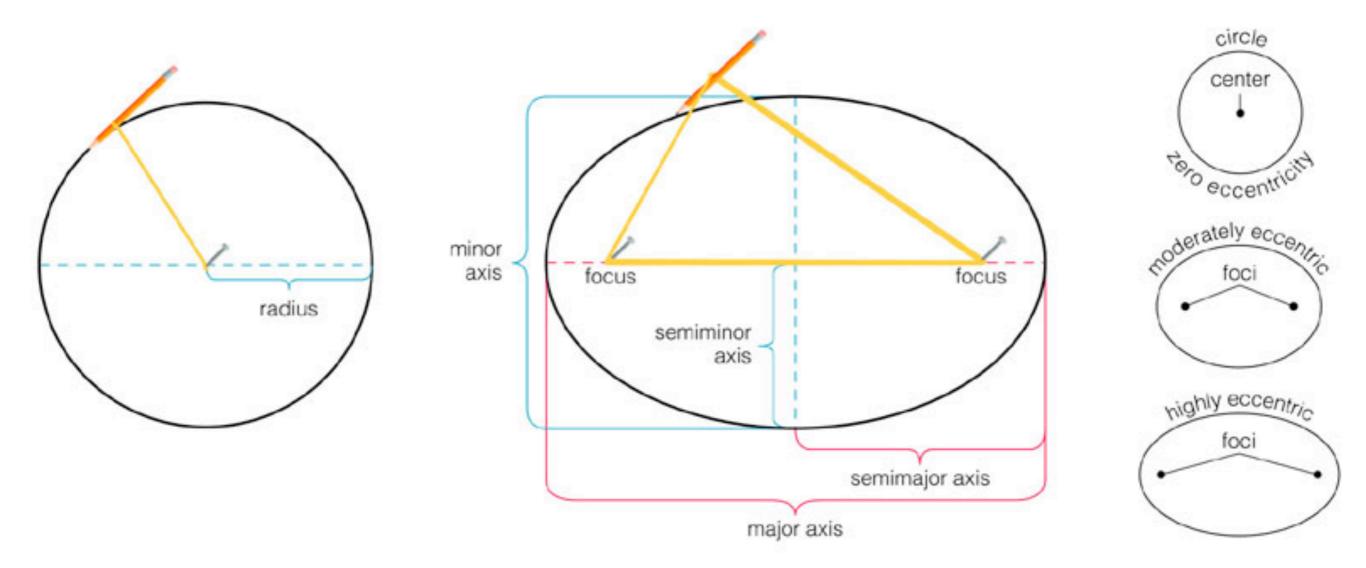
© 2008 W. H. Freeman and company icity measures the deviation of a circle

> As eccentricity e increases the shape elongates

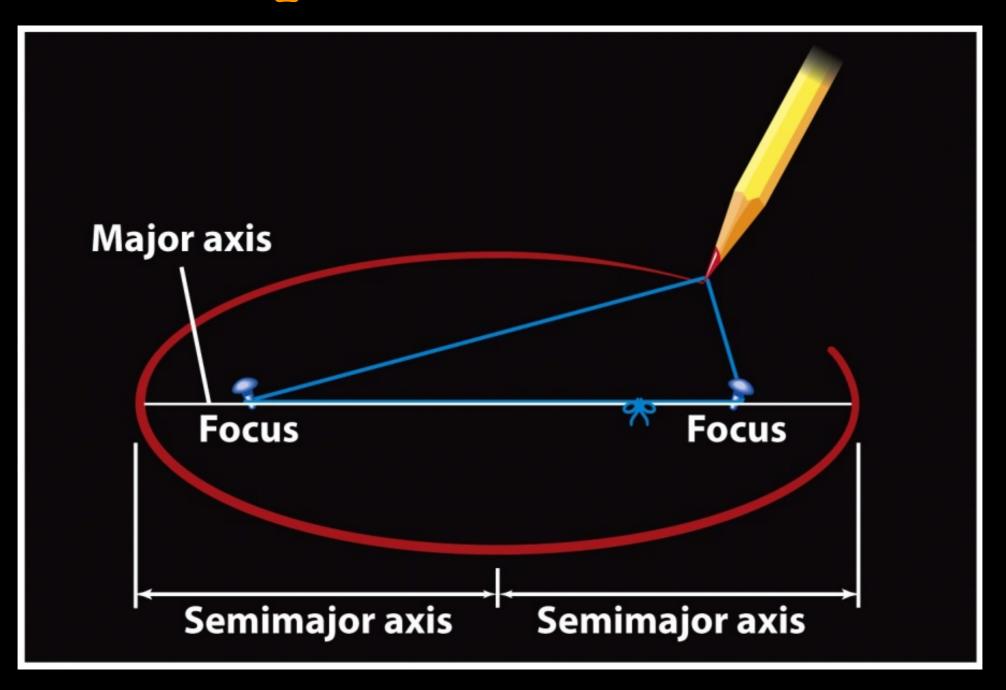


 \succ perihelion distance - distance closest to Sun

Geometry offeelipsses

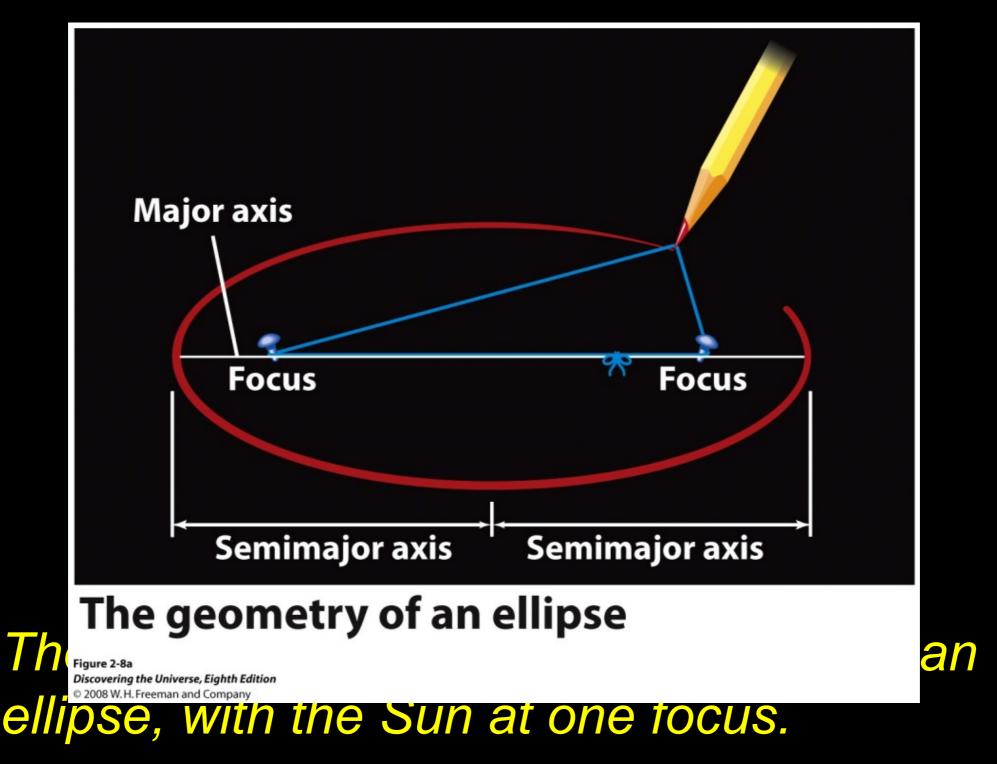


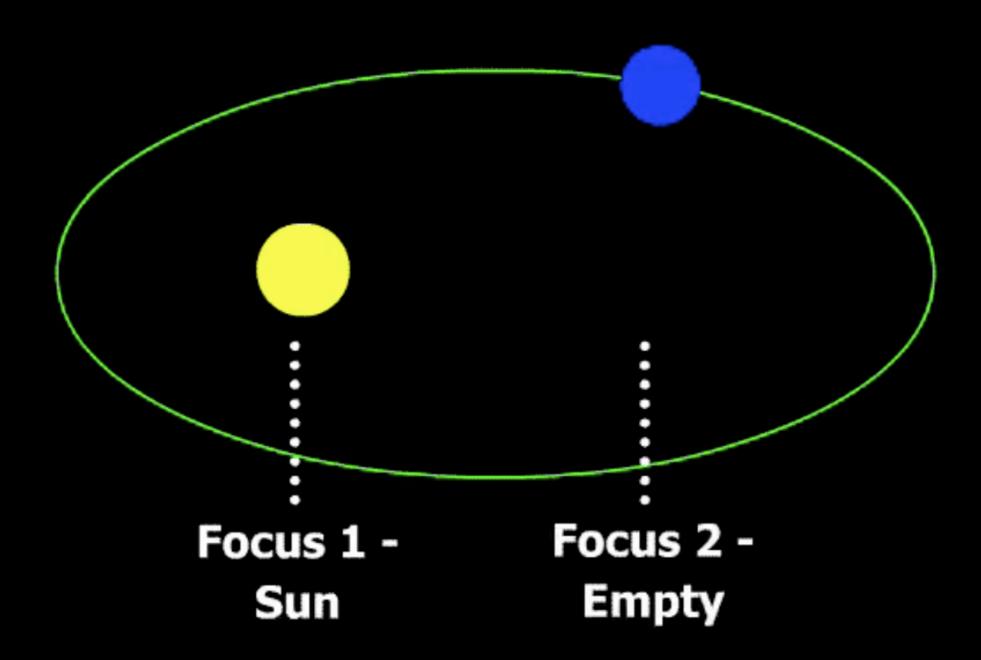
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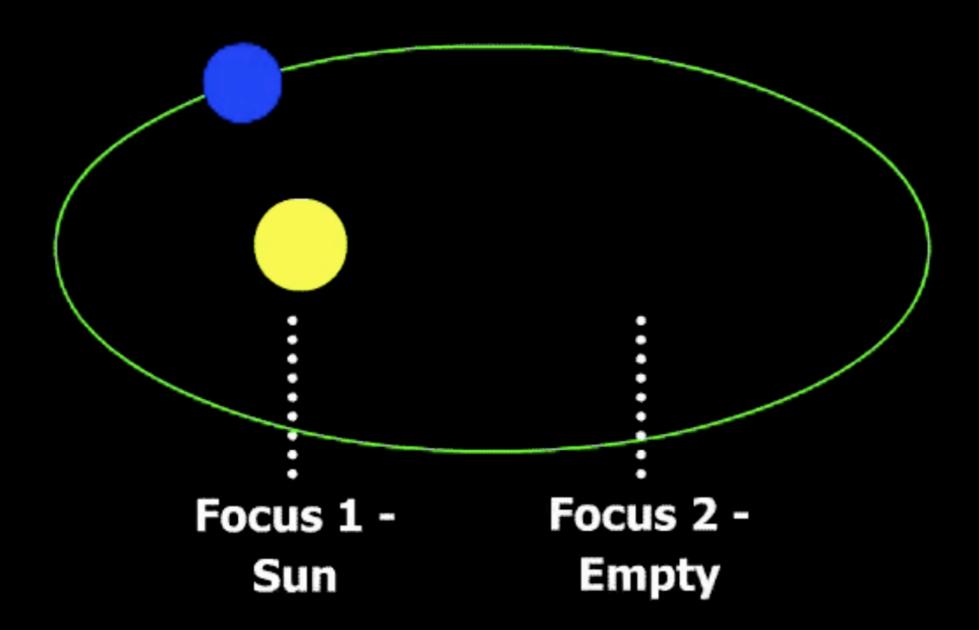


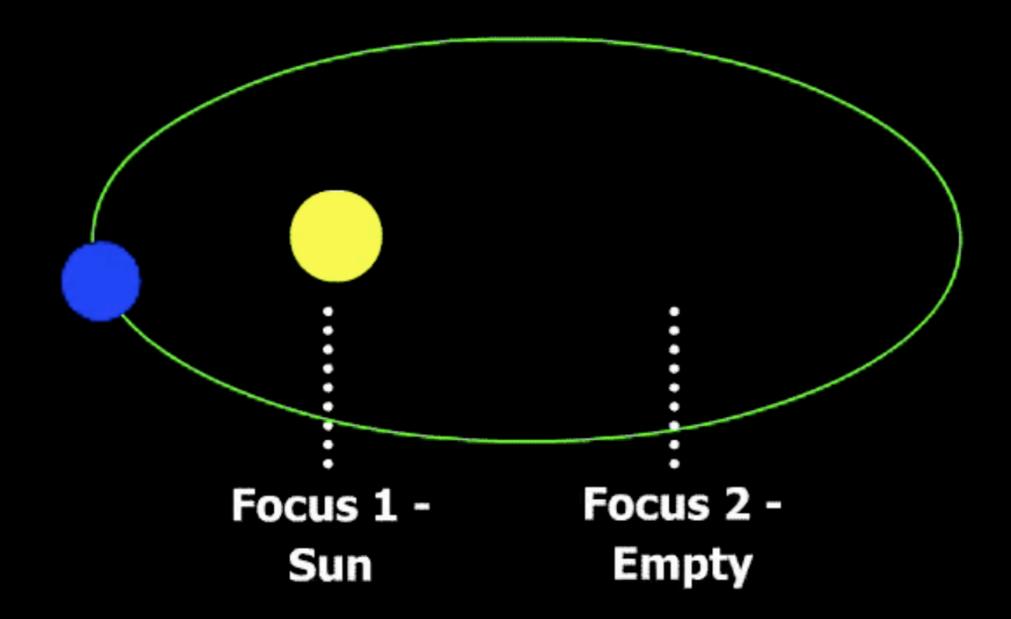
The orbit of a planet around the Sun is an ellipse, with the Sun at one focus

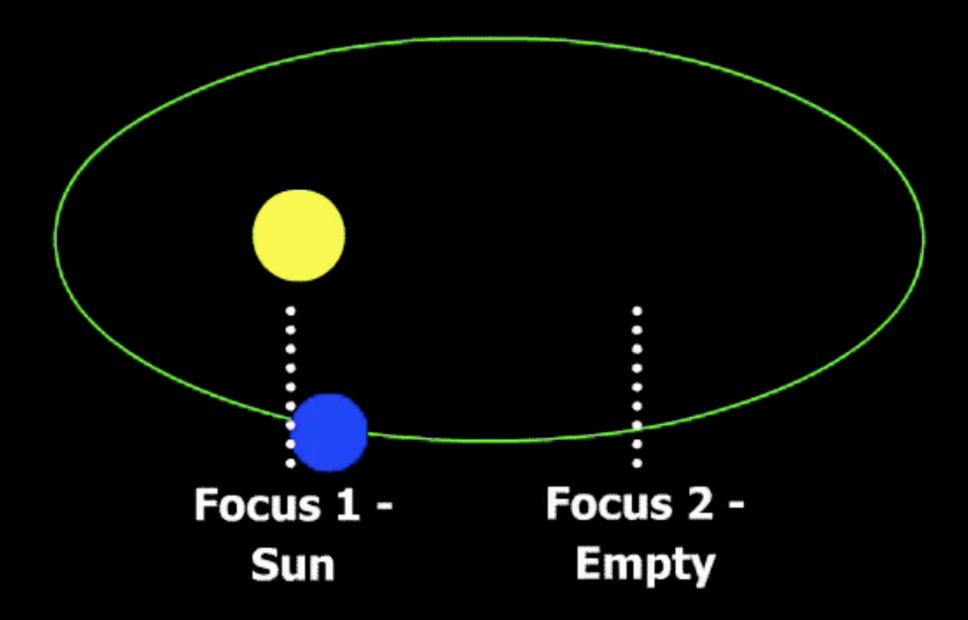
(See: http://astro.unl.edu/naap/pos/animations/kepler.swf)

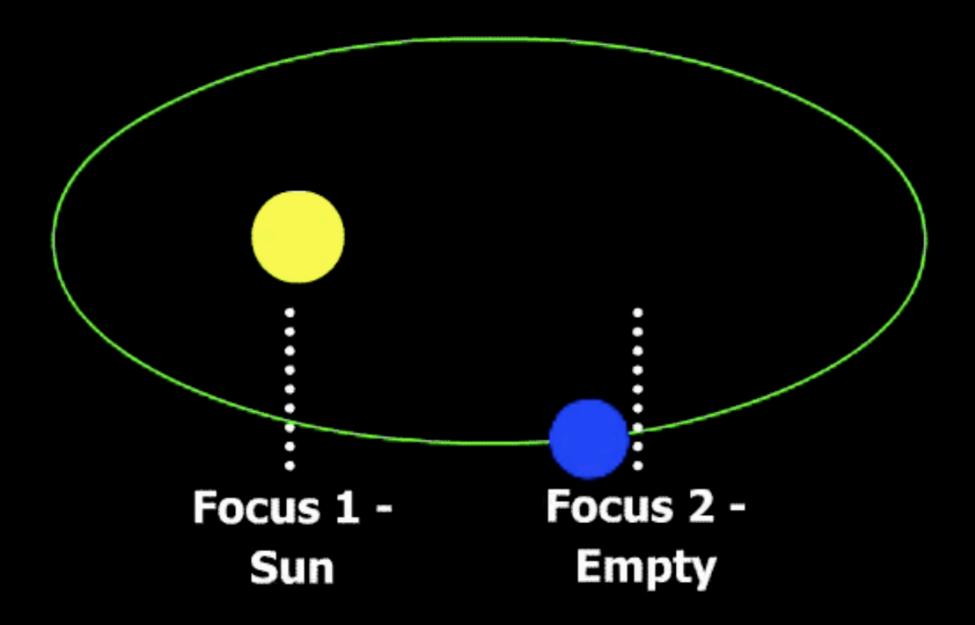


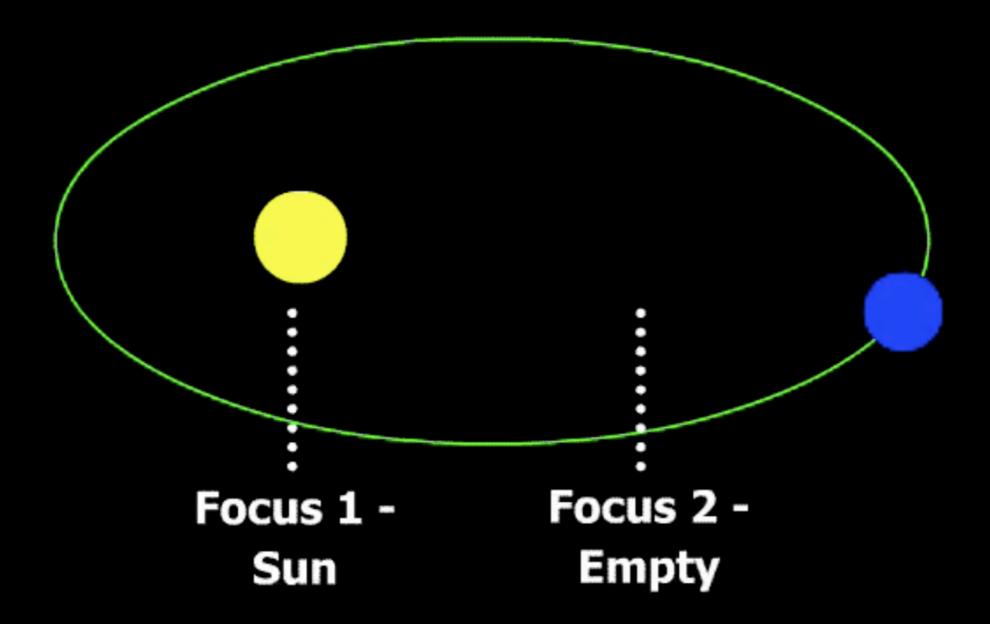


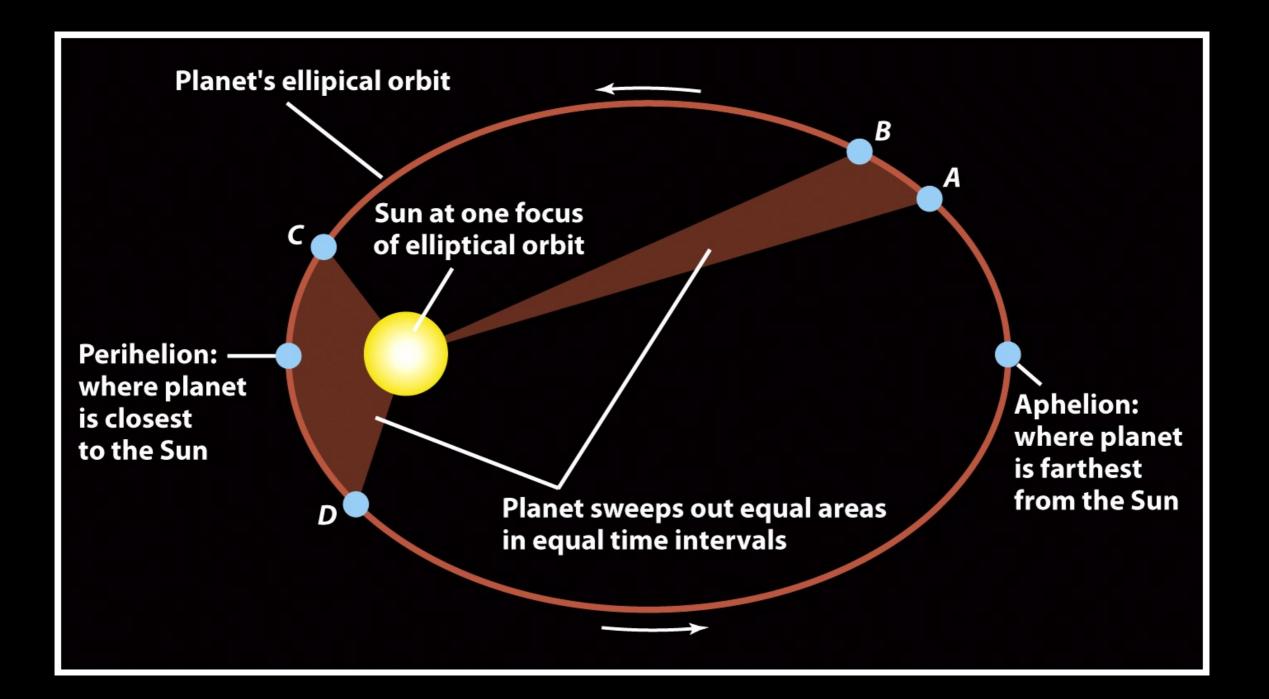






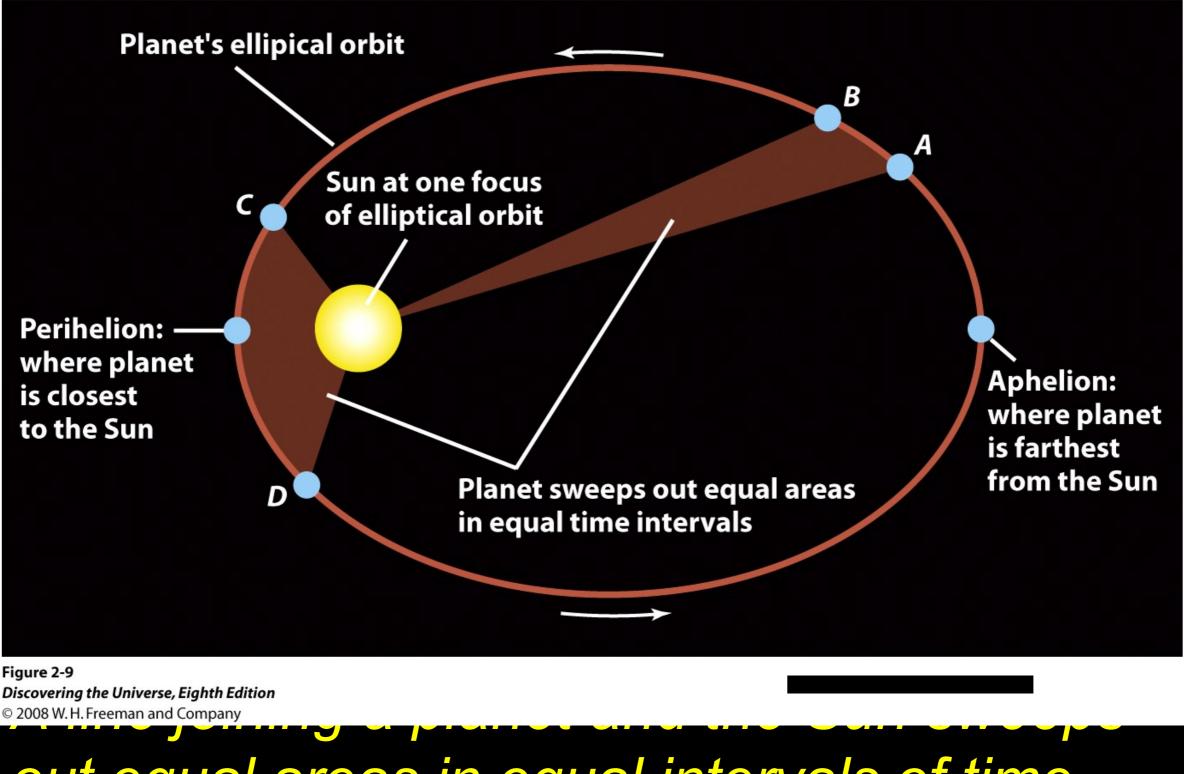




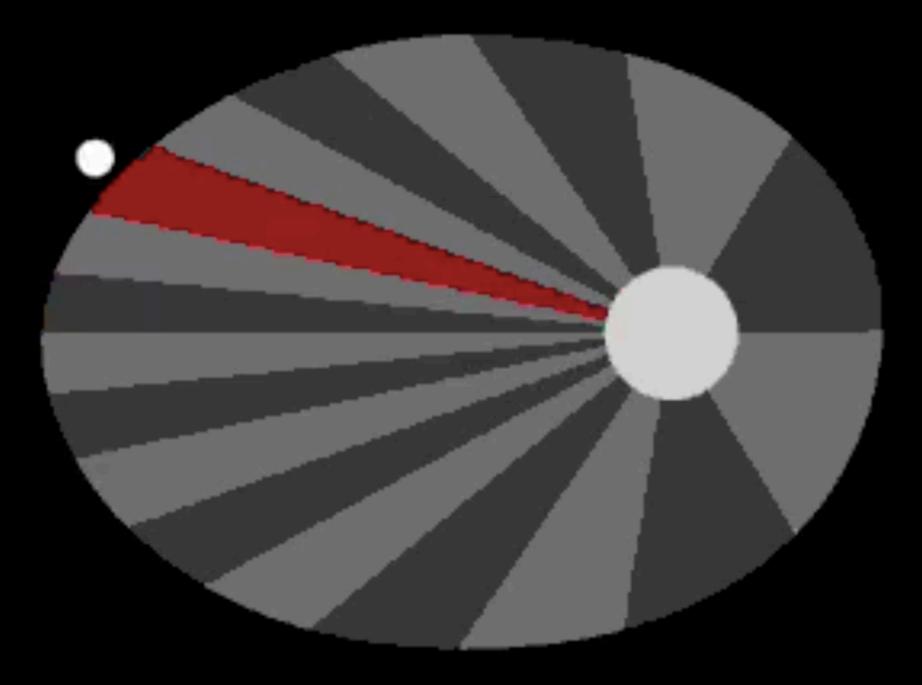


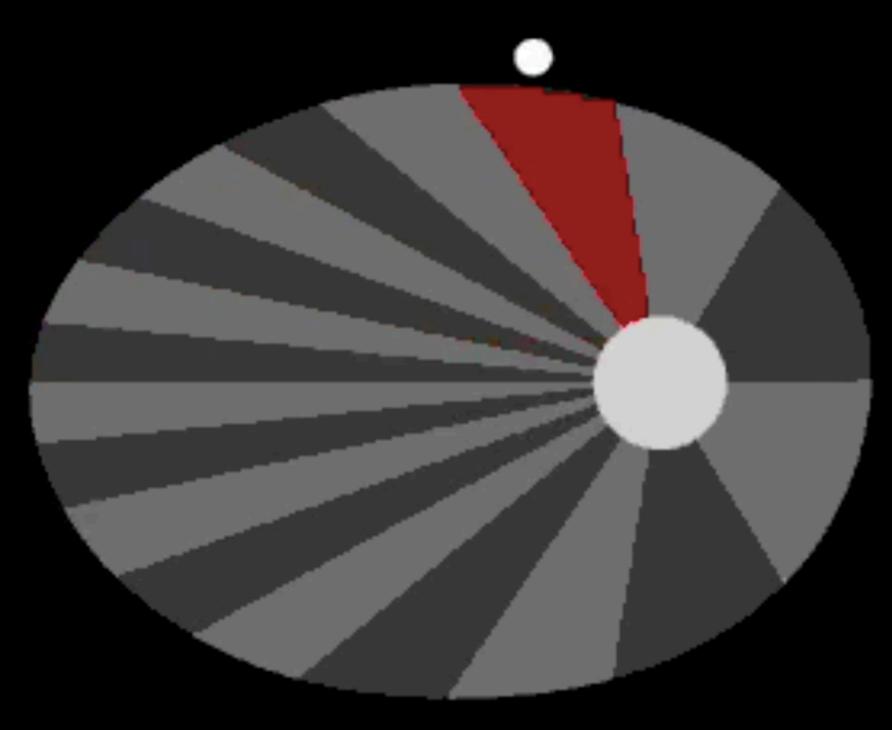
A line joining a planet and Sun sweeps out equal areas in equal intervals of time

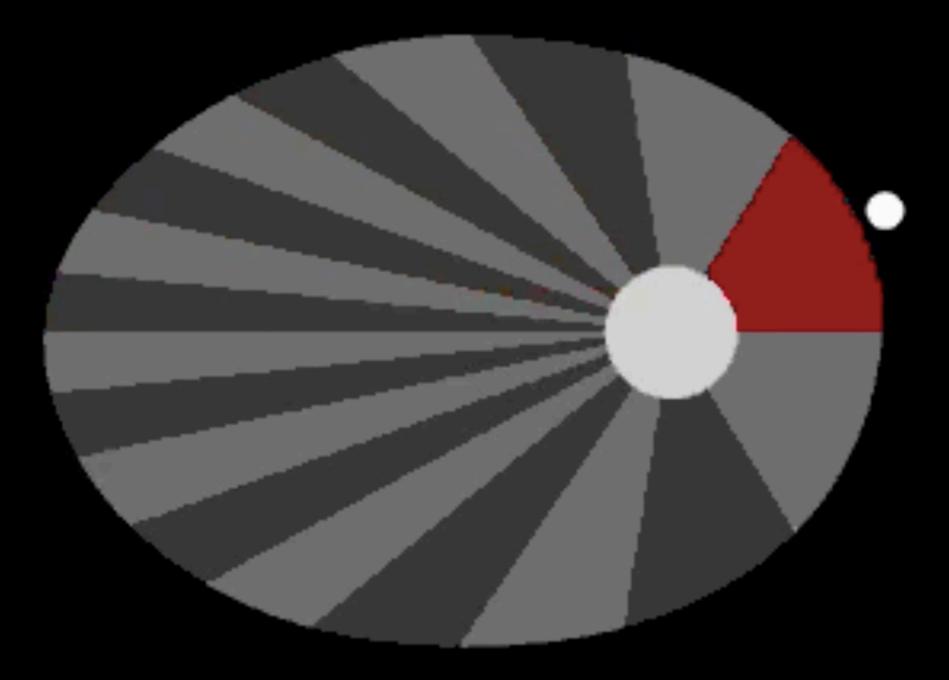
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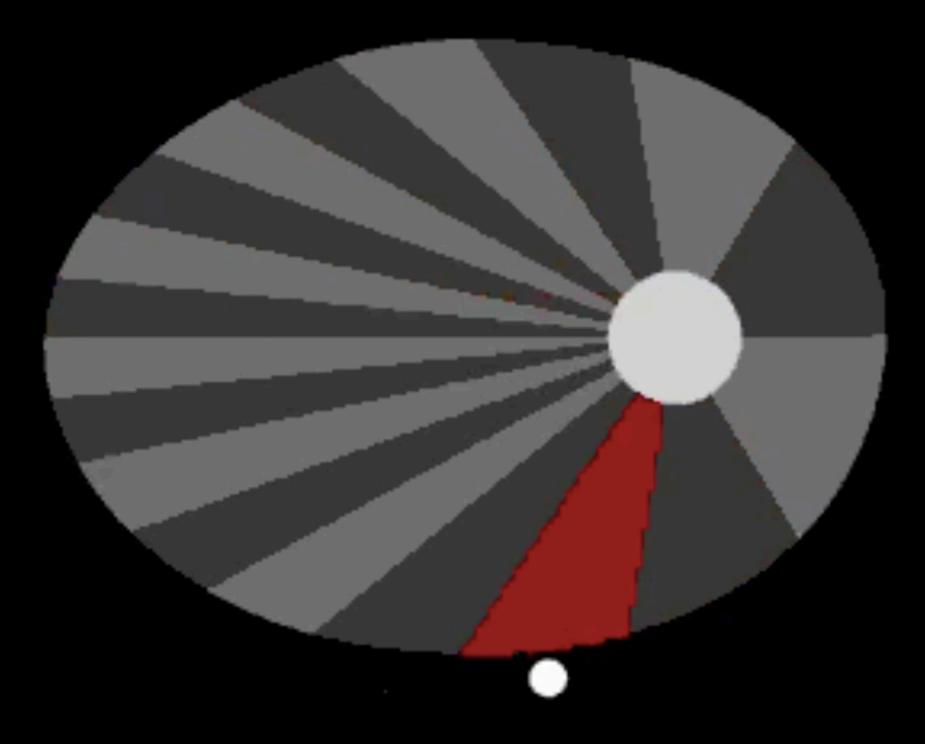


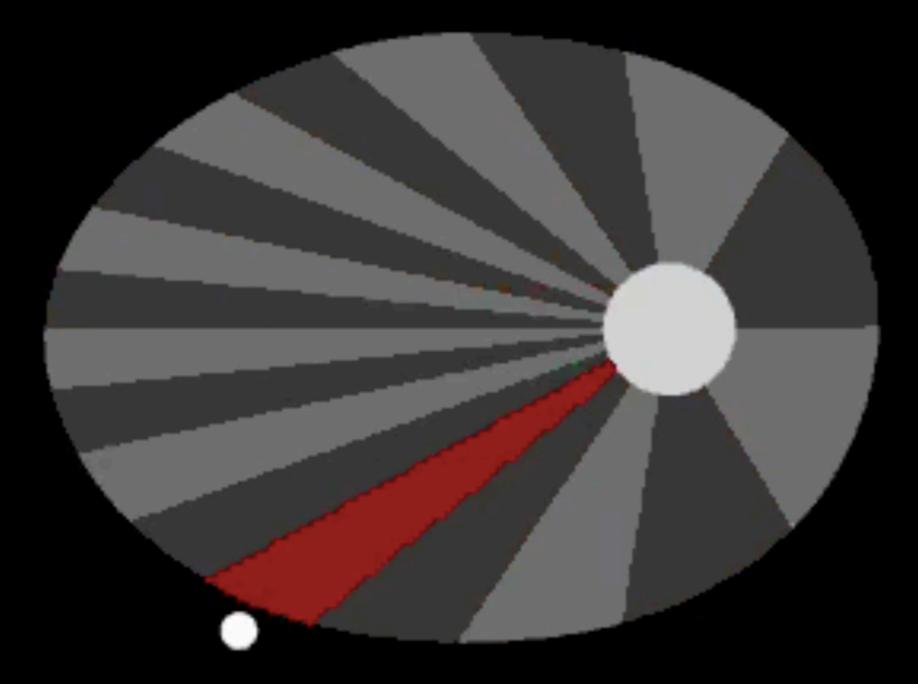
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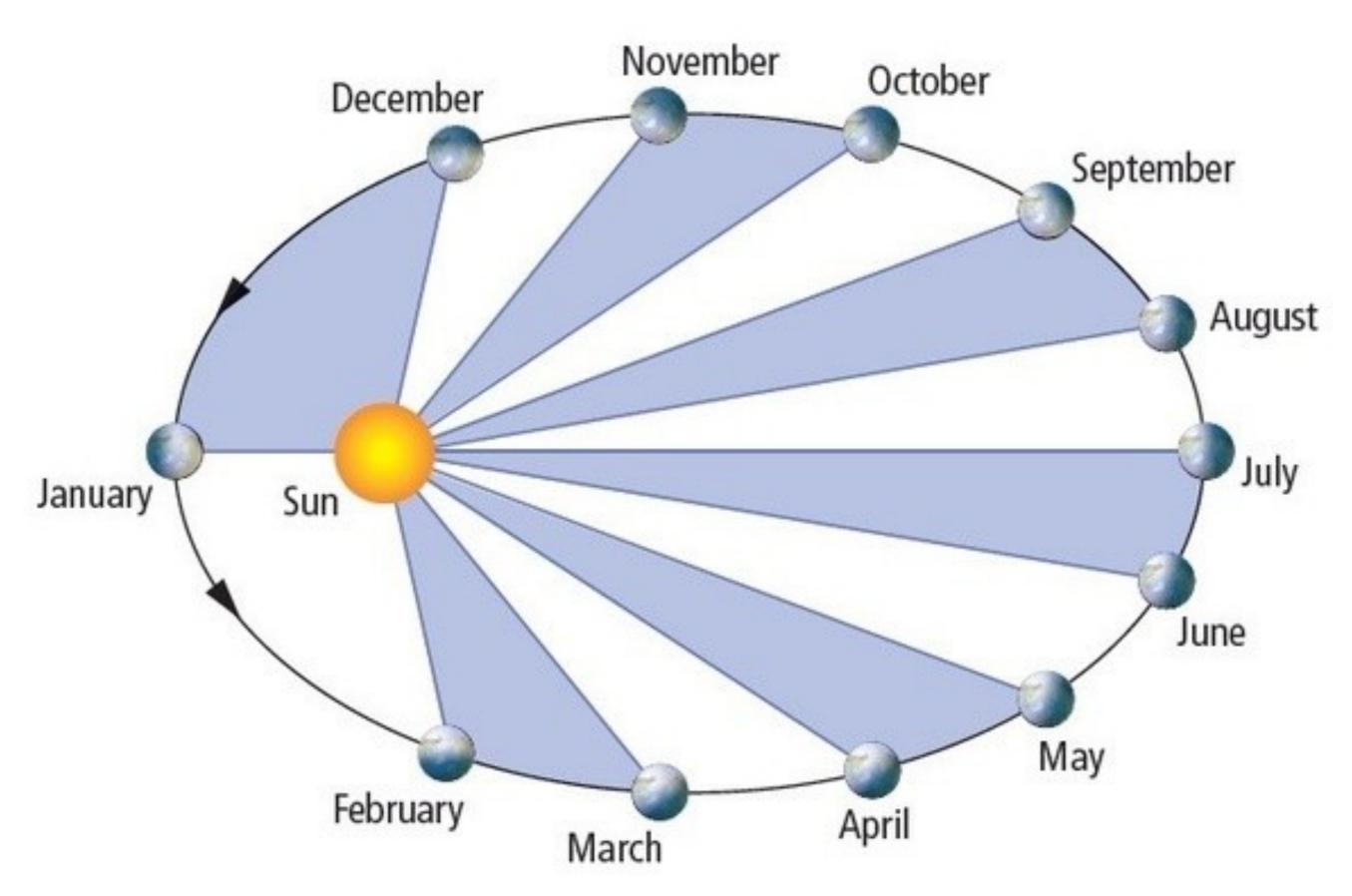




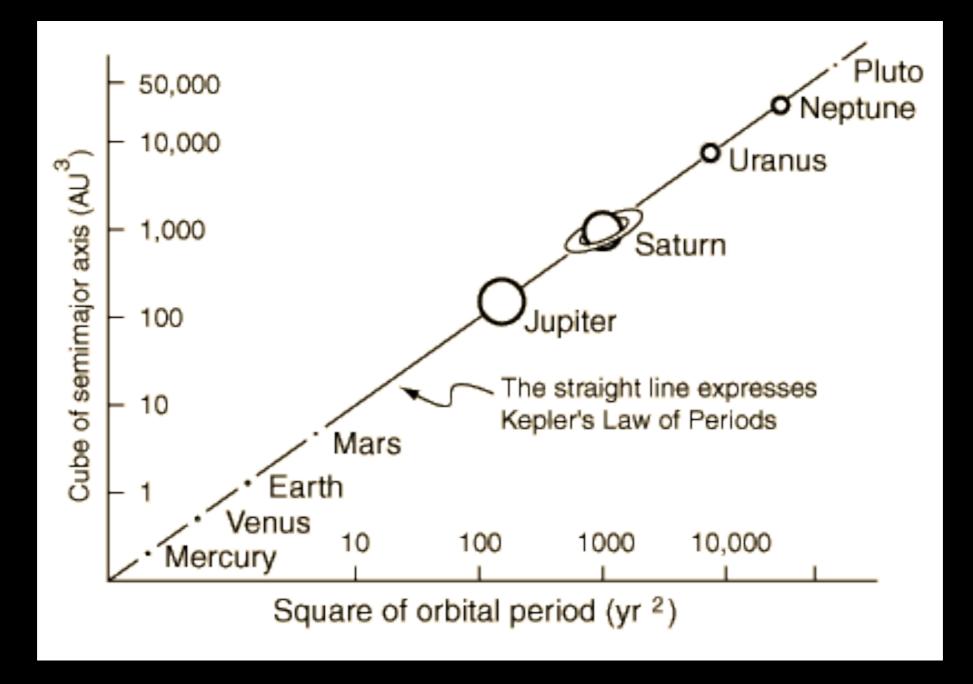








Kepler's Third Law



The square of a planet's sidereal period around the Sun is directly proportional to the cube of the length of its orbit's semimajor axis $(T^2 \propto R^3)$

Galileo Galilei (1564-1642)



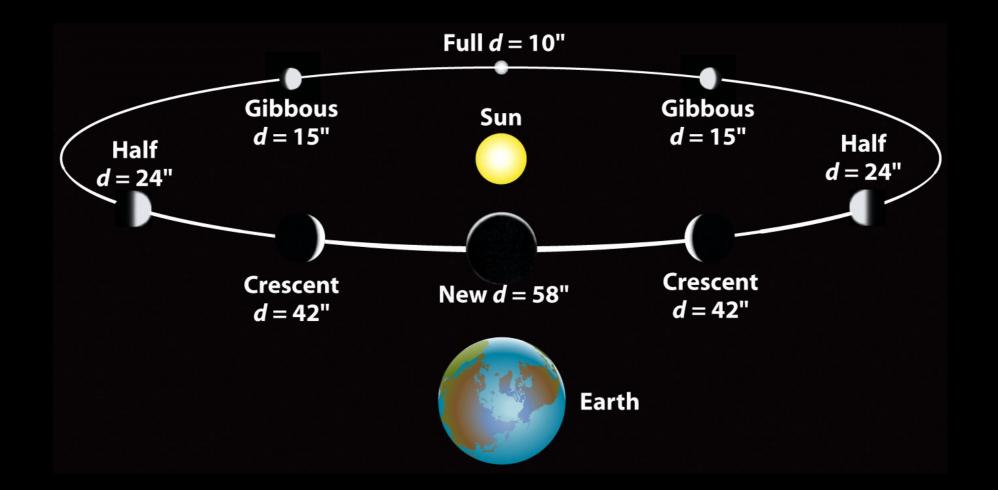
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Galileo Galilei

- Made many discoveries that supported heliocentric view and Kepler's laws
- Was the first to make use of and published results using a telescope
- > Discovered moons of Jupiter

> Discovered that Venus has phases

Galileo Observations of Venus



> Venus appears small at gibbous phase and large at crescent phase

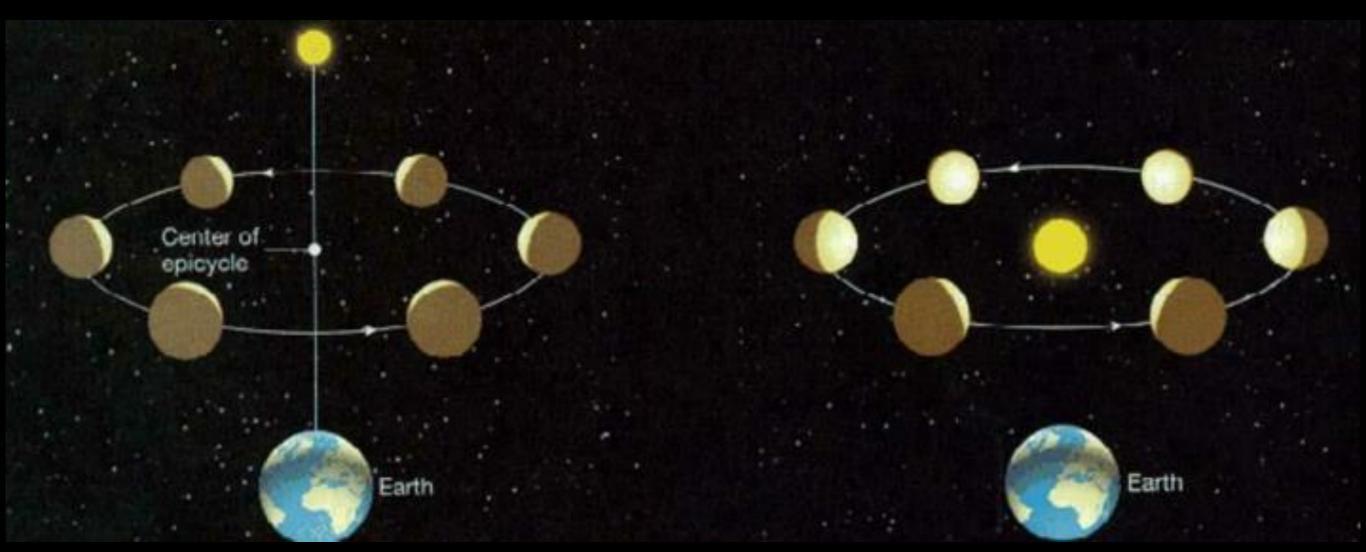
- Note: Ptolemaic model does not predict Gibbous nor Full phases

> d is diameter in units of arcsec

- the farther an object is the smaller its angular size

Phases of Venus

- In the Ptolemaic system (left), Venus always lies between the Sun and the Earth and it would always show a crescent phase
- The Copernican system (right) predicts a full range of phases for Venus as it passes from between the Sun and the Earth to being on the opposite side of the Sun from the Earth



- ➤ Because of orbital mechanics, a planet with a superior orbit (one that orbits the Sun further away than Earth) will not go through phases, as we see it, because the planet won't cast a shadow from our perspective
- Earth will go through phases from the point of view of any planet that has an orbit superior to earth
- > This extends to the relative position of any planet
- Somebody on Jupiter would see phases on Mars, but not on Saturn
- Somebody on Neptune could see phases on all seven of the other planets

- > Mars is a partial exception to the superior orbit rule
- You will not see phases on Mars from Mars' shadow of sunlight, but Mars is close enough to Earth that Earth's shadow can cause some partial phasing



- > This can make Mars appear irregular (or gibbous) because of Earth's interference with the light from the sun
- Planets further out into the solar system are too distant for Earth to interfere in this way

May 6, 2018



Discovered that Jupiter has moons

 \succ Confirmed orbits of moons obey Kepler's laws $(T^2 \propto R^3)$

39

What is the motion called when a planet seems to be moving westward in the sky?

- A. retrogade
- B. parallax
- C. reverse parallax

40

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In Copernican system, what is shape of planets' orbits?

- A. elipse
- B. parabola
- C. circle

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On what planet does a "year" last only 88 days?

- A. Mars
- B. Mercury
- C. Jupiter

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- **B.** Mercury
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In what year did Galileo first use an optical telescope to study the moon?

- A. 250 BCE
- B. 1611
- C. 1945

In what year did Galileo first use an optical telescope to study the moon?

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47 Galileo discovered something about Venus with his

telescope that shook the old theories.

Which of the following was Galileo's discovery?

A. Venus surface is similar to Earth

B. Venus has phases like the moon

C. Venus has rings

48 Galileo discovered something about Venus with his

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Which of the following was Galileo's discovery?

A. Venus surface is similar to Earth

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Heliocentric means around:

A. Sun

B. Earth

C. Moon

D. Jupiter

49

50

Heliocentric means around:

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B. Earth

C. Moon

D. Jupiter

The greatest distance of a planet from the sun is called what? Is it the planet's:

A. aphelion

B. perihelion

C. helix

D. eccentricity

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According to Kepler's Laws, the cube of the mean distance of a planet from the sun is proportional to the:

- A. area that is swept out
- B. cube of the period
- C. square of the period
- D. fourth power of the mean

According to Kepler's Laws, the cube of the mean distance of a planet from the sun is proportional to the:

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According to Kepler's Laws, all orbits of the planets are:

- A. ellipses
- B. parabolas
- C. hyperbolas
- D. squares

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A. ellipses

- B. parabolas
- C. hyperbolas
- D. squares

With a telescope here on Earth, would we ever see Venus

in a crescent phase?

A. Yes

With a telescope here on Earth, would we ever see Venus

in a crescent phase?

A. Yes

With a telescope here on Earth, would we ever see

Jupiter in a crescent phase?

A. Yes

60

With a telescope here on Earth, would we ever see Jupiter in a crescent phase?

A. Yes

⁶¹ QUERY 3

- (i) Mars is 1.5 AU away from the Sun. What is its orbital period?
- (*ii*) Jupiter's mean orbital radius is 5.2 AU. What is the period of Jupiter's orbit around the Sun?
- [AU is the abbreviation for astronomical units, where 1 AU = 1.5 \times 10^{11} m is the mean Earth-Sun distance]

62 QUERY 3

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Kepler's law $\blacktriangleright R^3 = KT^2$

Since Earth is at 1 AU and it takes 1 year to go around the Sun $rac{K}{K} = \frac{AU^3}{Vr^2}$

(i) Period of Mars is
$$\blacksquare$$
 $T = \sqrt{R^3/K} = 1.84 \text{ yr}$

(*ii*) Period of Jupiter is $r T = \sqrt{R^3/K} = 11.85 \text{ yr}$

⁶³ QUERY 4

Earth has an orbital period of 365 days and its mean distance from the Sun is 1.495×10^8 km. The Pluto's mean distance from the Sun is 5.896×10^9 km. Using Kepler's third law, calculate Pluto's orbital period in Earth days

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What we know $r T_E = 365 \text{ days}$ $r_E = 1.495 \times 10^8 \text{ km}$ $r_P = 5.896 \times 10^9 \text{ km}$

$$\left(\frac{T_E}{T_P}\right)^2 = \left(\frac{r_E}{r_P}\right)^3 \qquad T_P =?$$

$$\left(\frac{365 \ days}{T_P}\right)^2 = \left(\frac{1.495 \times 10^8 \ km}{5.896 \times 10^9 \ km}\right)^3 \qquad T_P = 9.00 \times 10^4 \ days$$

$$\left(\frac{365 \ days}{T_P}\right)^2 = (2.54 \times 10^{-2})^3 \qquad T_P = 9.00 \times 10^4 \ days$$

$$\left(\frac{1.32x10^5 \ days^2}{{T_P}^2}\right) = 1.63x10^{-5}$$

$$T_P = \sqrt{\frac{1.32x10^5 \ days^2}{1.63x10^{-5}}}$$